

# Reconstruction of muon bundles in **KM3NeT** detectors using machine learning methods

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2015/18/E/ST2/00758

We gratefully acknowledge the funding support by program “Excellence initiative—research university” for the AGH University in Krakow as well as the ARTIQ project: UMO-2021/01/2/ST6/00004 and ARTIQ/0004/2021.

# Outline

2

Introduction

```
graph TD; A[Introduction] --> B[Muon event reconstruction]; B --> C[Summary];
```

Muon event reconstruction

Summary

# Outline

3

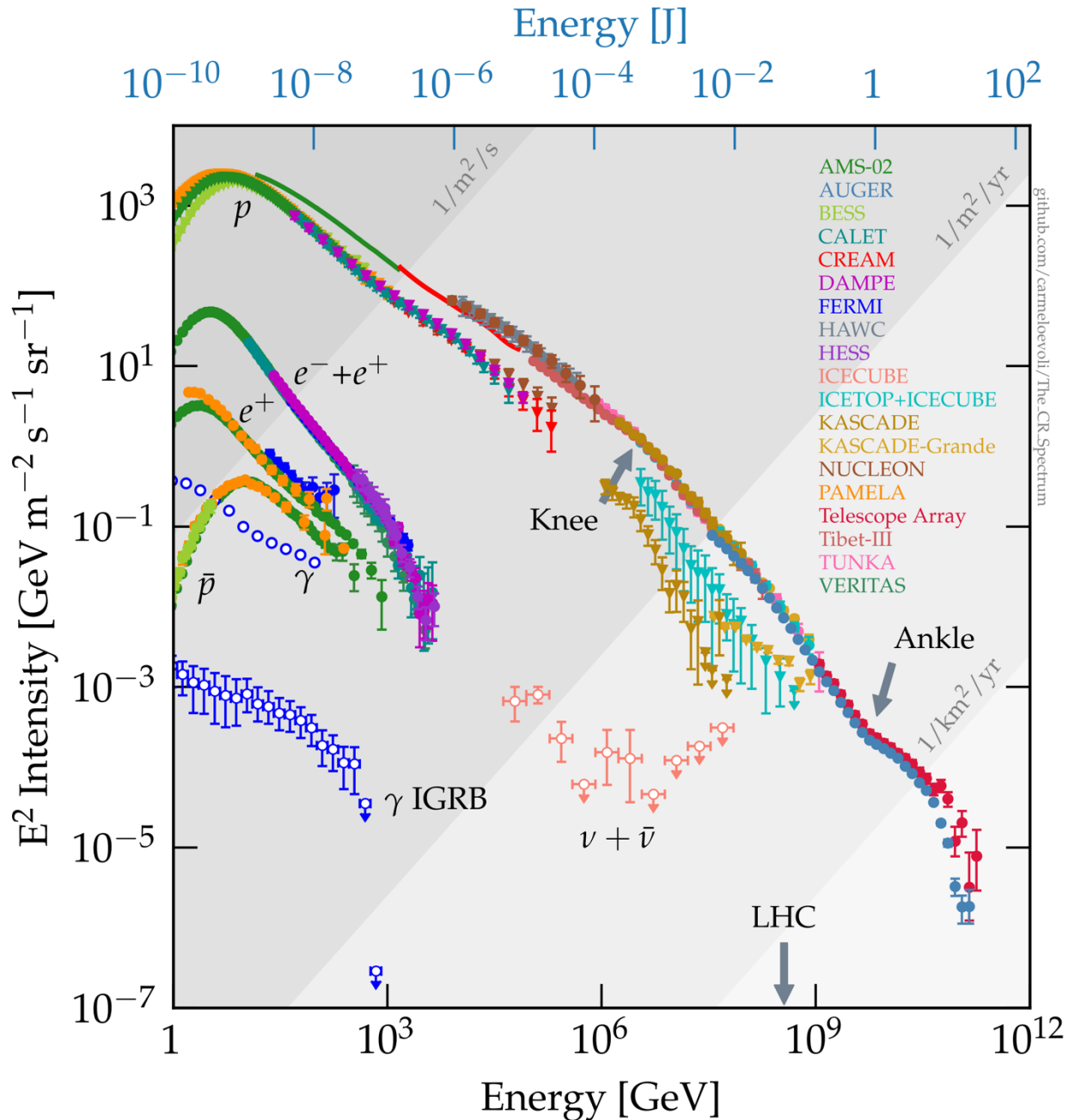
Introduction

Cosmic rays

KM3NeT

Muon event reconstruction

Summary



Cosmic rays (CR):

High-Energy particles and atomic nuclei from outer space that reach the Earth

Discovered by Victor Hess in 1912  
(Nobel Prize in 1936)

Quite a few measurements since then ...

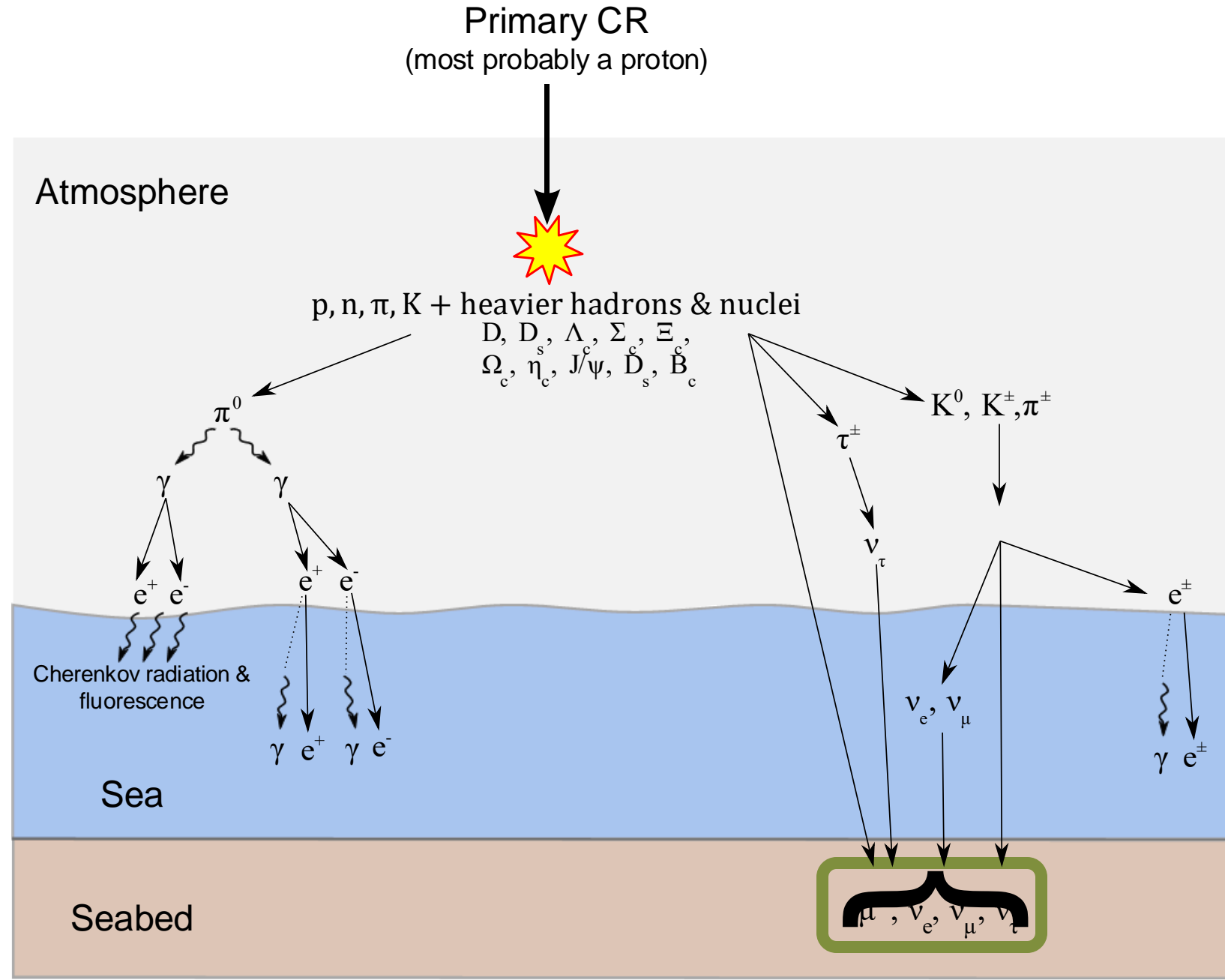
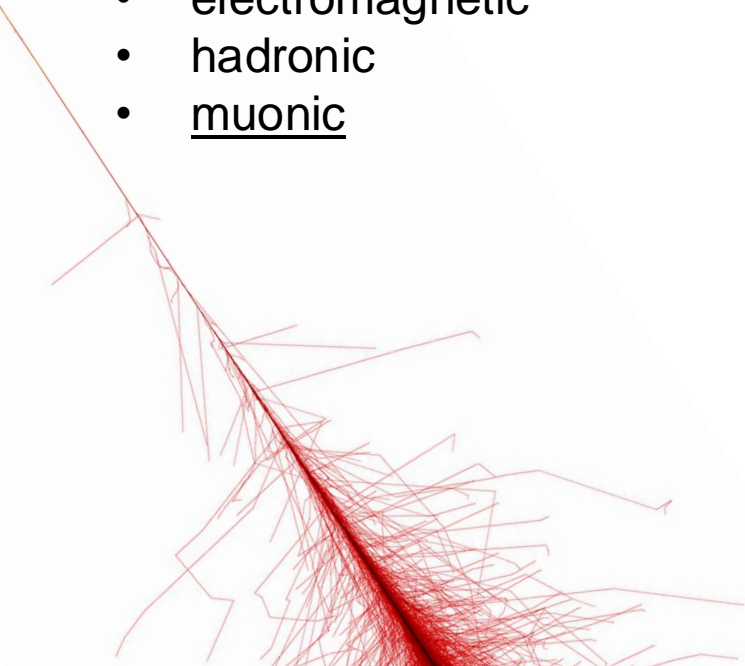
But wait, muons are not in the figure ... !?

Muons are not primary CRs!

They are secondaries produced in ...

## Extensive air showers (EAS):

- ❖ Caused by primary CR
- ❖ Most start at  $h \sim 30 - 40 \text{ km}$
- ❖ 3 components:
  - electromagnetic
  - hadronic
  - muonic



# Outline

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Introduction

Cosmic rays

KM3NeT

Muon event reconstruction

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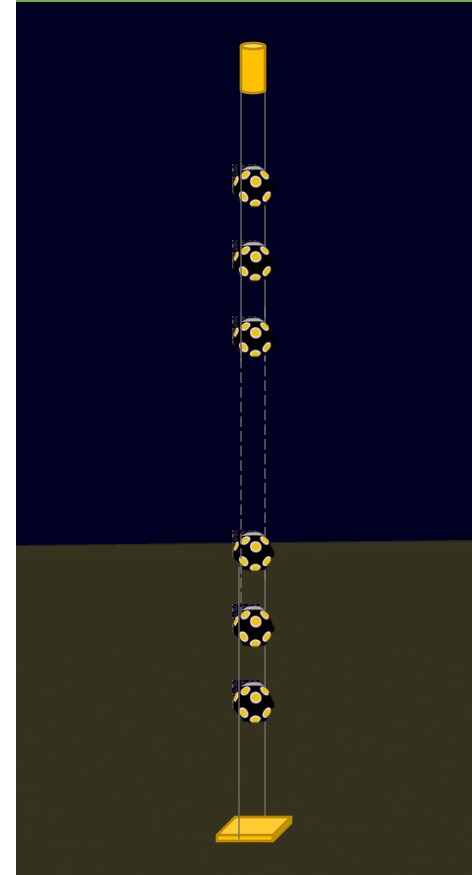
DOM:  
71 unique components



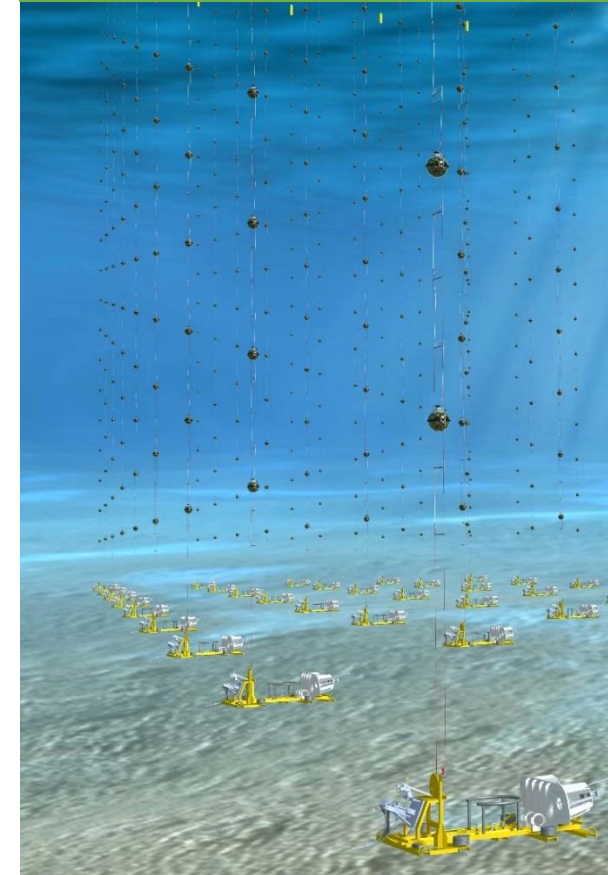
1 DOM:  
31 PMTs



1 string (DU):  
18 DOMs



1 building block:  
115 DUs



[DOM production: \(@Nikhef\)](#)



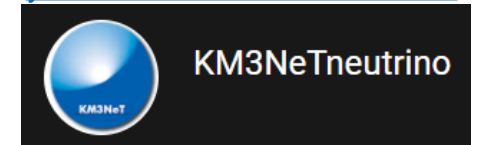
[Preparation for deployment:](#)



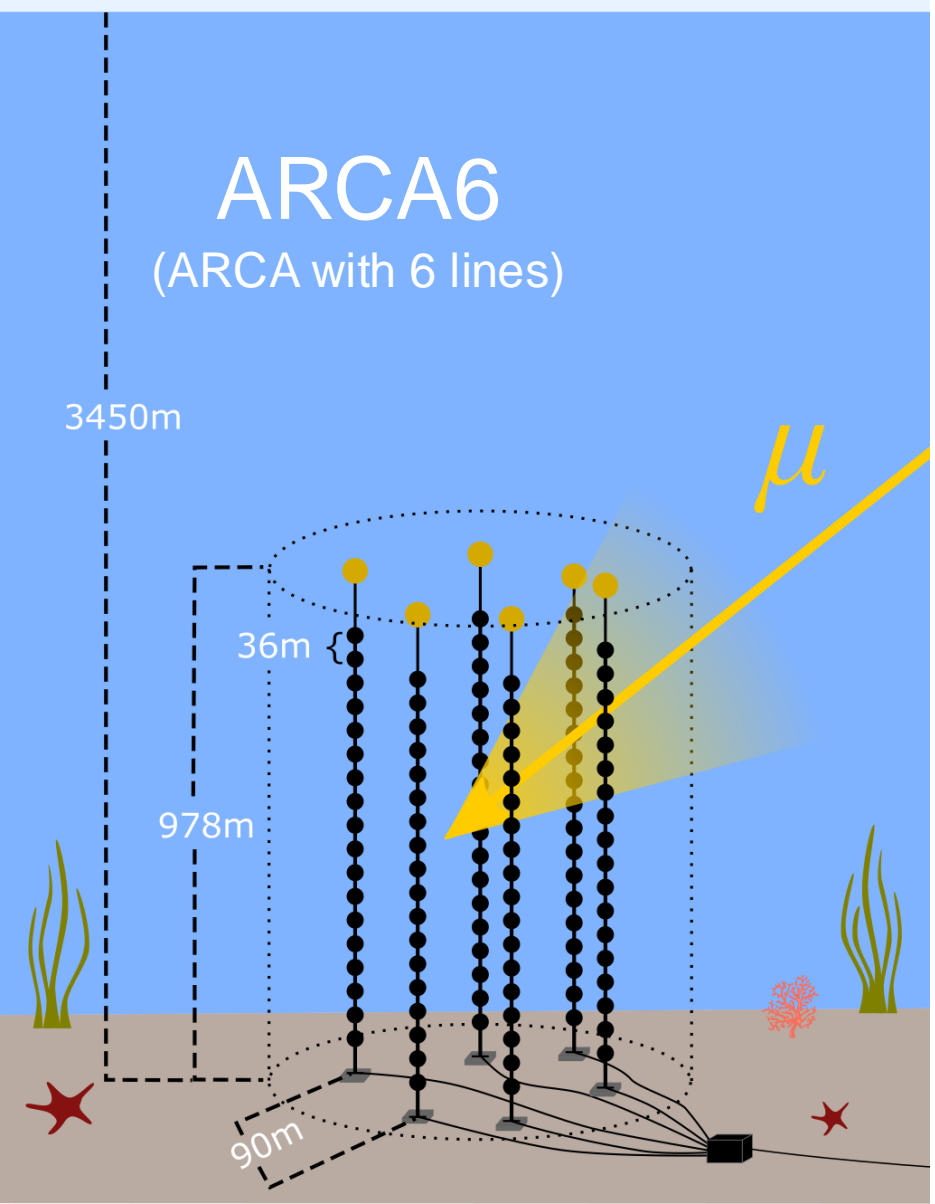
[String deployment:](#)



More at:  
[youtube.com/KM3NeTneutrino](https://youtube.com/KM3NeTneutrino)

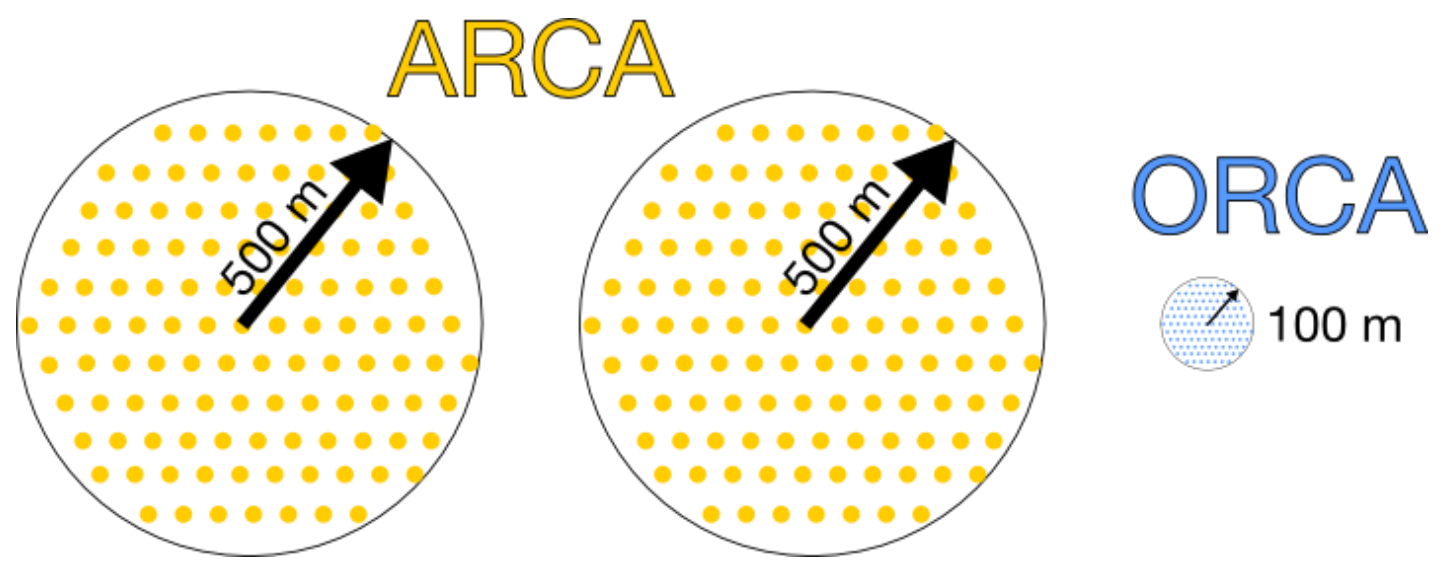






Detector	ARCA	ORCA
Depth	3.5 km	2.45 km
Volume	1 km <sup>3</sup> (1Gton)	0.007 km <sup>3</sup> (7Mton)
# lines	28 / 2x115	18 / 115
Topic	Astroparticle RCA*	Oscillation RCA*
Goal	$\nu_{\text{astro}}$	$m_\nu$ hierarchy

\*RCA : Research with Cosmics in the Abyss





## ARCA timeline



Dec 2015: first strings

•

... [more details](#)



Sep 2023: +9 **strings**



Currently: **ARCA28!**

•

...



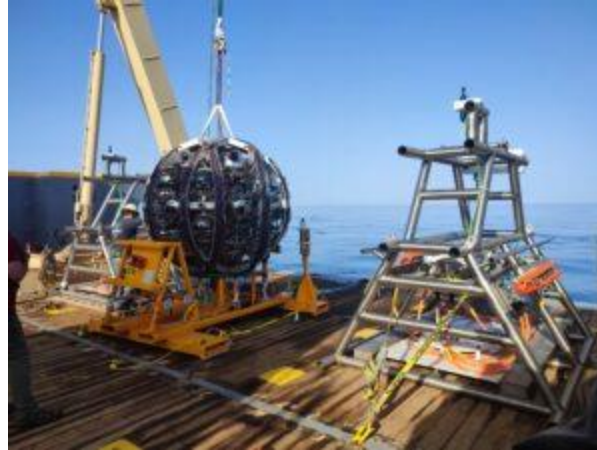
Sep 2024: next deployment

•

...



Nov 2031(?): ARCA2x115



For more follow us at:

<https://www.km3net.org>



## ORCA timeline



Dec 2017: first strings

•

... [more details](#)



Jun 2024: +4 **strings**



Currently: **ORCA22!**

•

...



Summer 2024: next deployment

•

...



Jan 2031(?): ORCA115



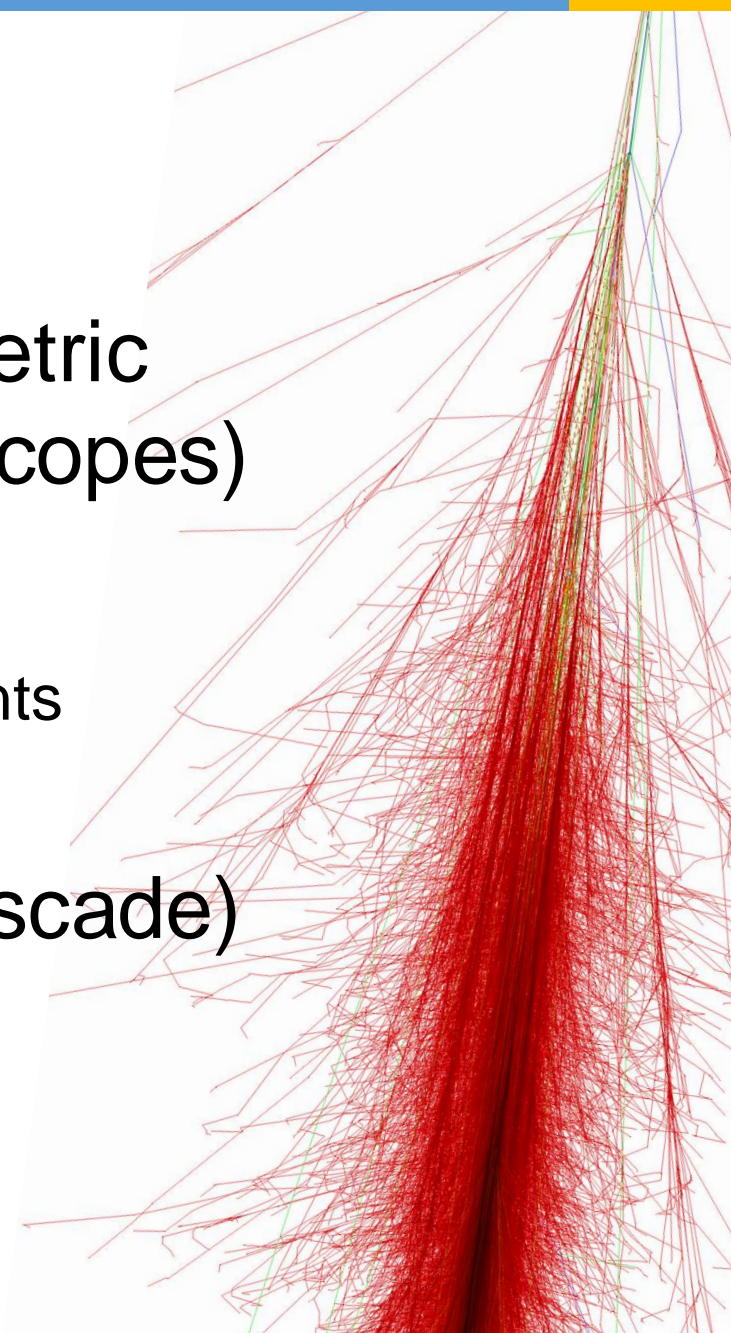
We have 2 options:

1. [MUPAGE](#) (atmospheric **MU**ons from **PA**rametric formulas: a fast **GE**nerator for neutrino telescopes)

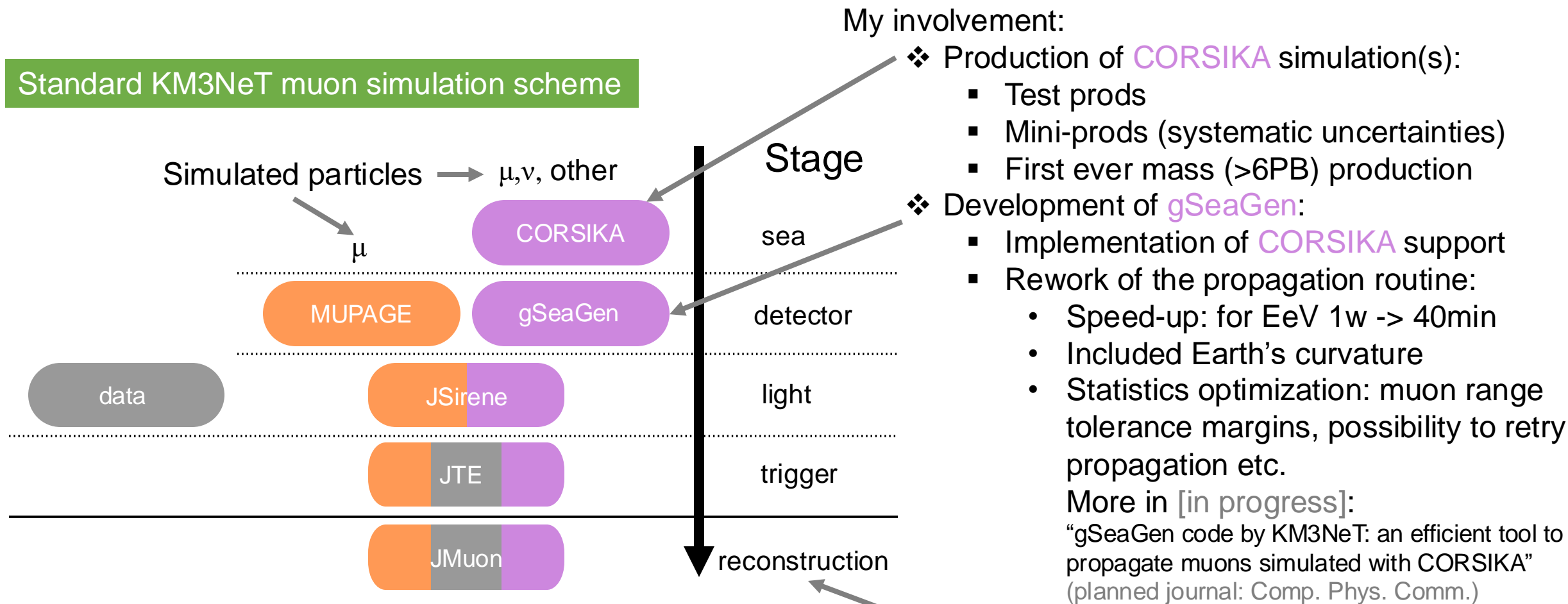
- developed for ANTARES
- fast muon MC generator
- based on parametric formulas and MACRO measurements
- parameters can be freely tuned

2. [CORSIKA](#) (**CO**smic **R**ay **SI**mulations for **KA**scade)

- developed for KASCADE
- full simulation of air showers
- customizable (models, primaries, etc.)



## Standard KM3NeT muon simulation scheme



My involvement:

- ❖ Production of **CORSIKA** simulation(s):
  - Test prods
  - Mini-prods (systematic uncertainties)
  - First ever mass (>6PB) production
- ❖ Development of **gSeaGen**:
  - Implementation of **CORSIKA** support
  - Rework of the propagation routine:
    - Speed-up: for EeV 1w -> 40min
    - Included Earth's curvature
    - Statistics optimization: muon range tolerance margins, possibility to retry propagation etc.
- More in [in progress]:  
 "gSeaGen code by KM3NeT: an efficient tool to propagate muons simulated with CORSIKA"  
 (planned journal: Comp. Phys. Comm.)
- ❖ Reconstruction of new observables  
 (see next Section)

Legend:

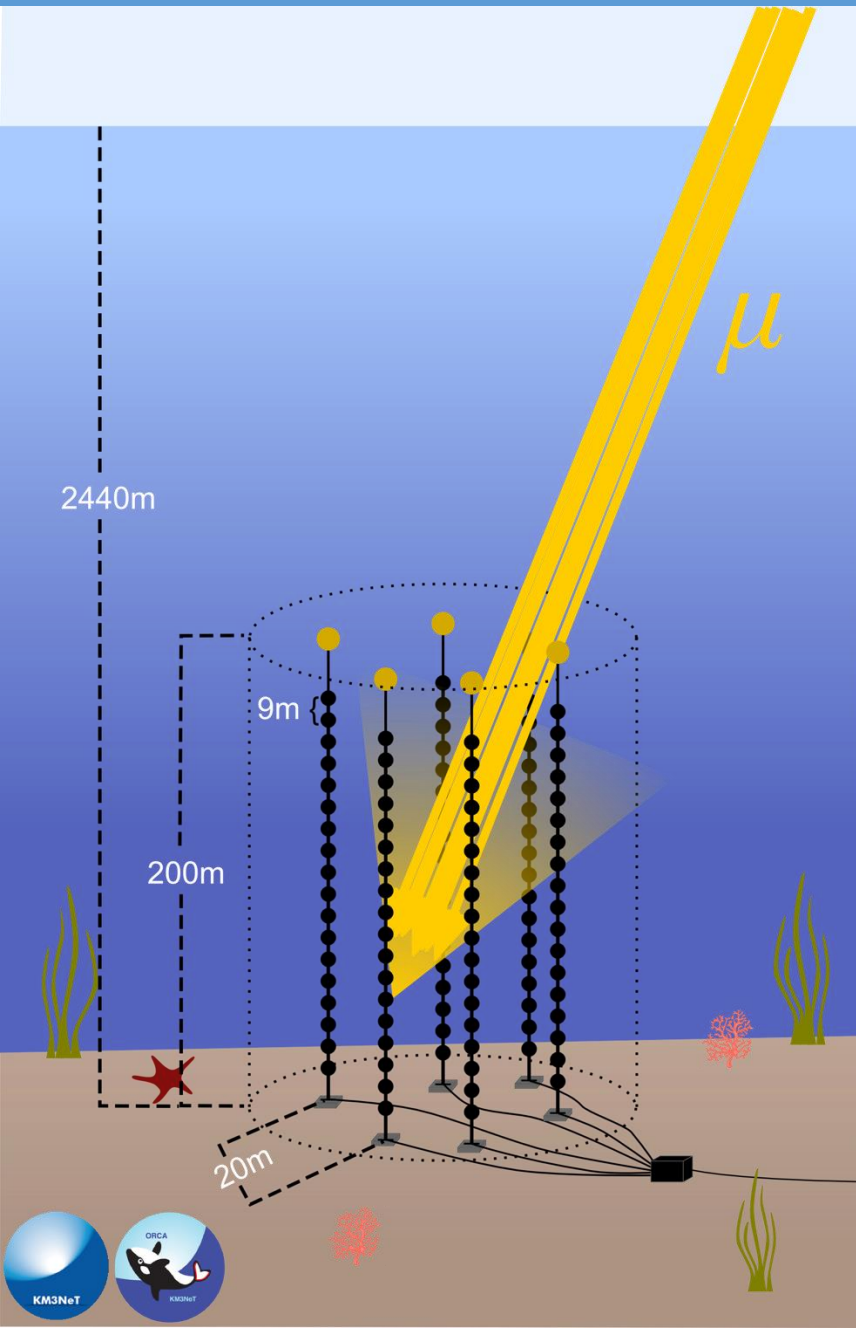
**sea** – sea surface above km3net detectors

**detector** – cylindrical volume around the detector

**light** – simulation of photon emission and detection near the detector (including environmental background)

**trigger** – selection of potentially interesting events e.g. 3DMuon selects muon tracks

**reconstruction** – reconstruction of various observables, e.g. energy, direction



Muon bundle: muons originating from a single EAS

Some important properties:

Observable	Description	Standard reco?
$\cos \theta_{\text{zenith}} = \frac{\sum \cos \theta_{\text{zenith}}}{N_{\mu}}$	Direction (zenith)	good
$E_{\text{bundle}} = \sum E_{\mu}$	Bundle energy	rather bad (focused on bundles with a single muon)
$E_{\text{primary}}$	Energy of the primary CR	no
$N_{\mu}$	Muon multiplicity	no

That's what I focused on

# Outline

Introduction



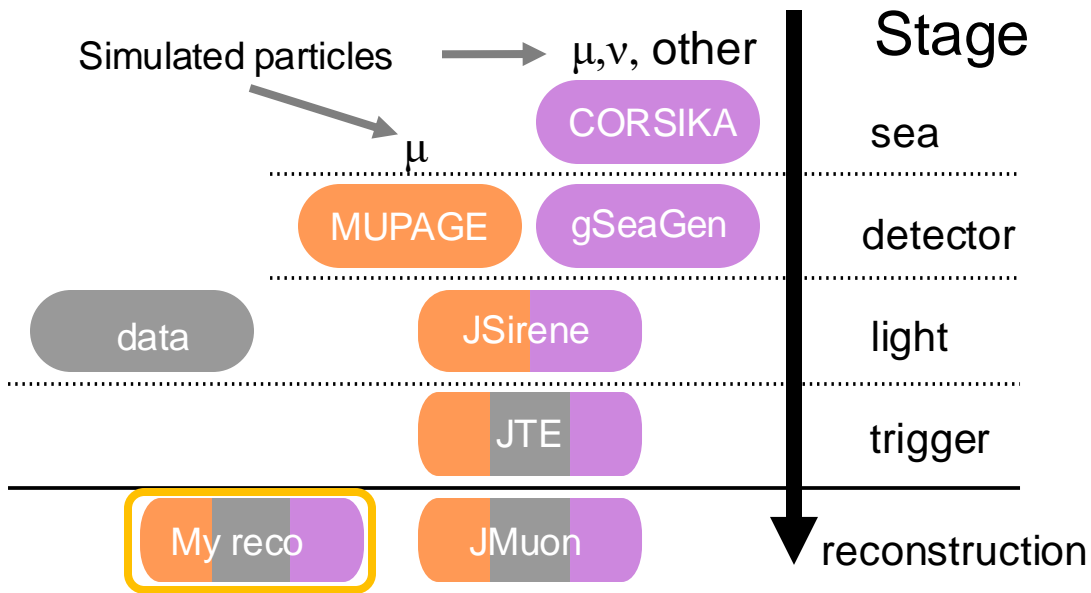
Muon event reconstruction



Summary



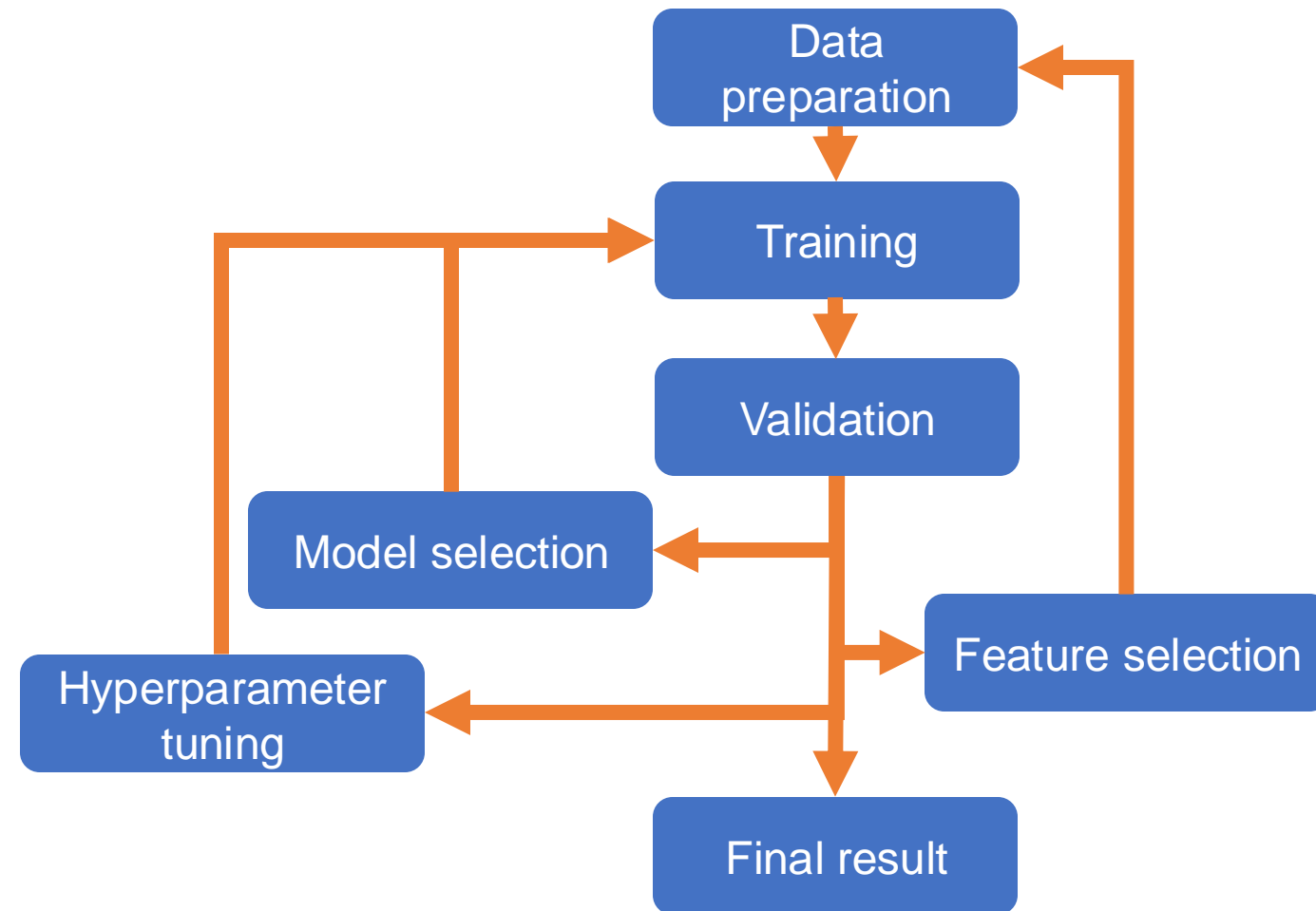
## KM3NeT muon simulation scheme

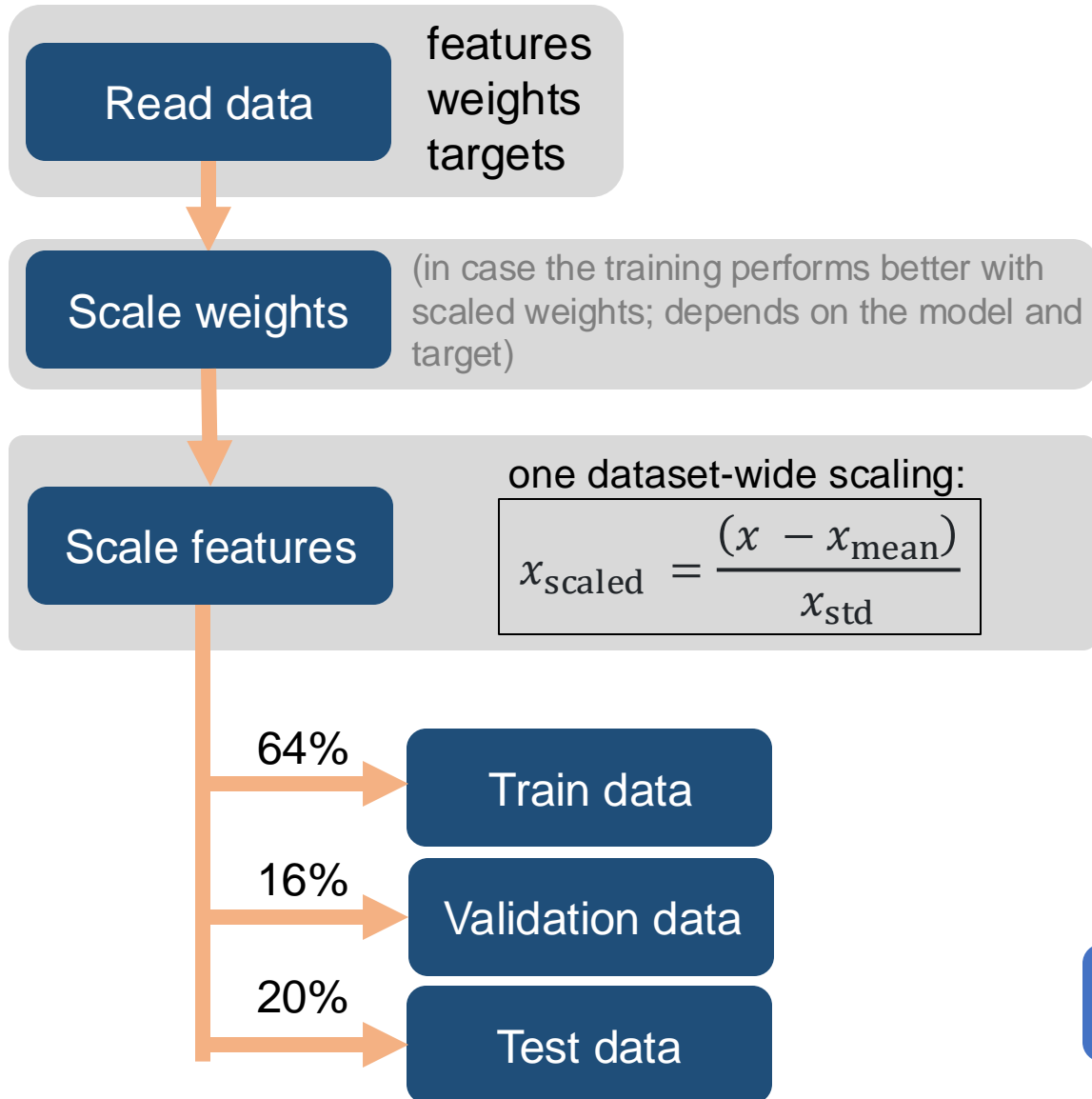


(some)  
Tools:

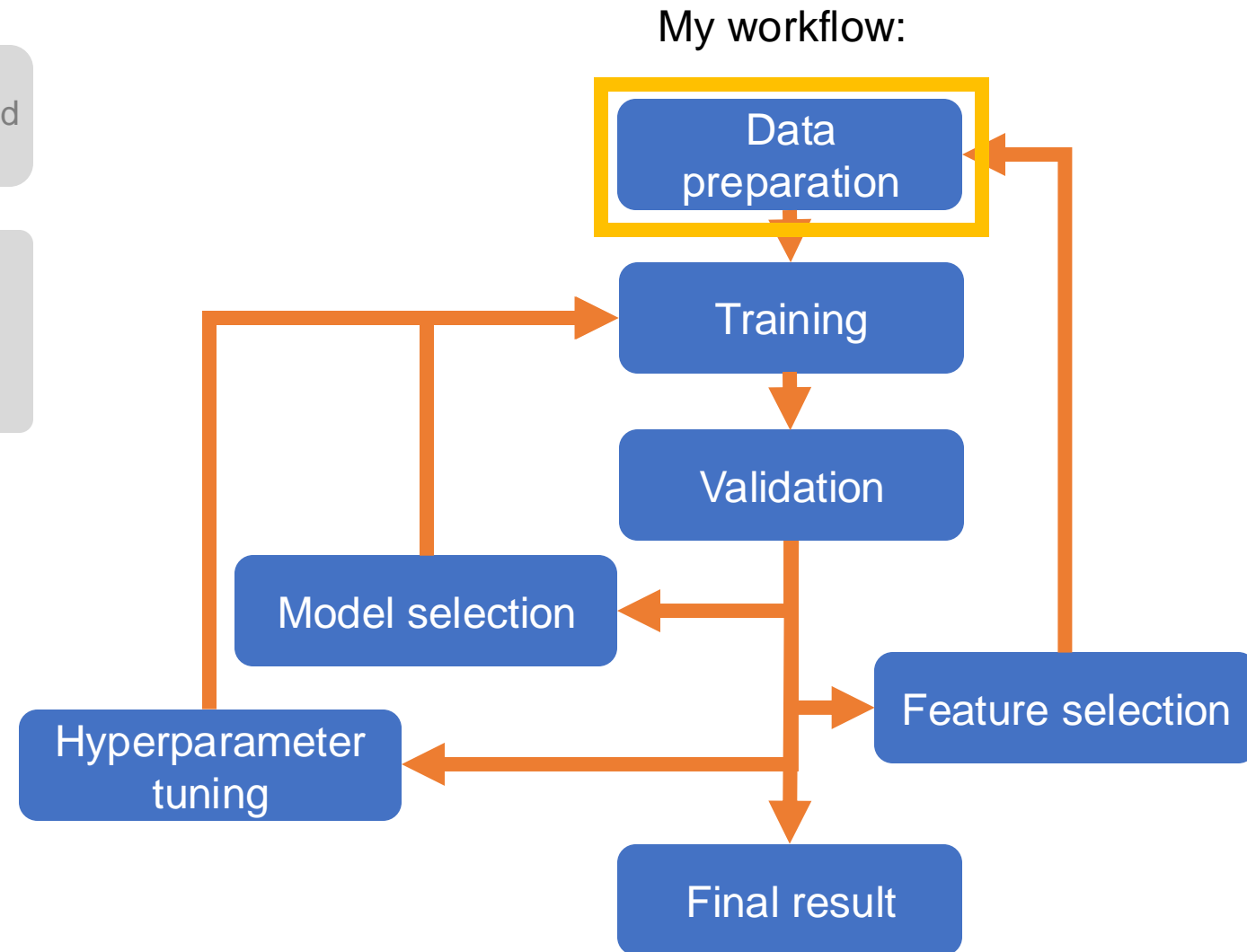


My workflow:

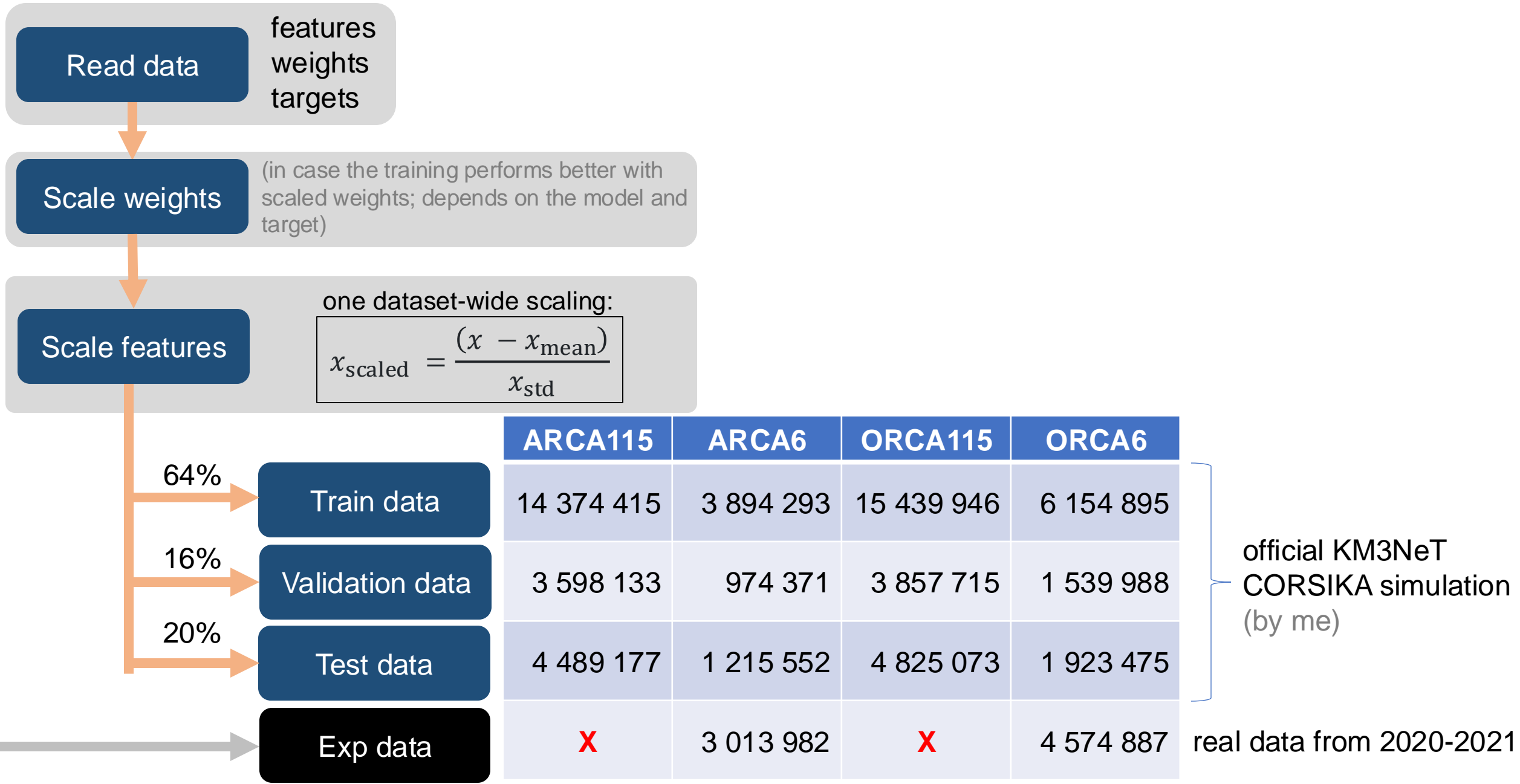




90% of success: feature engineering & preprocessing!

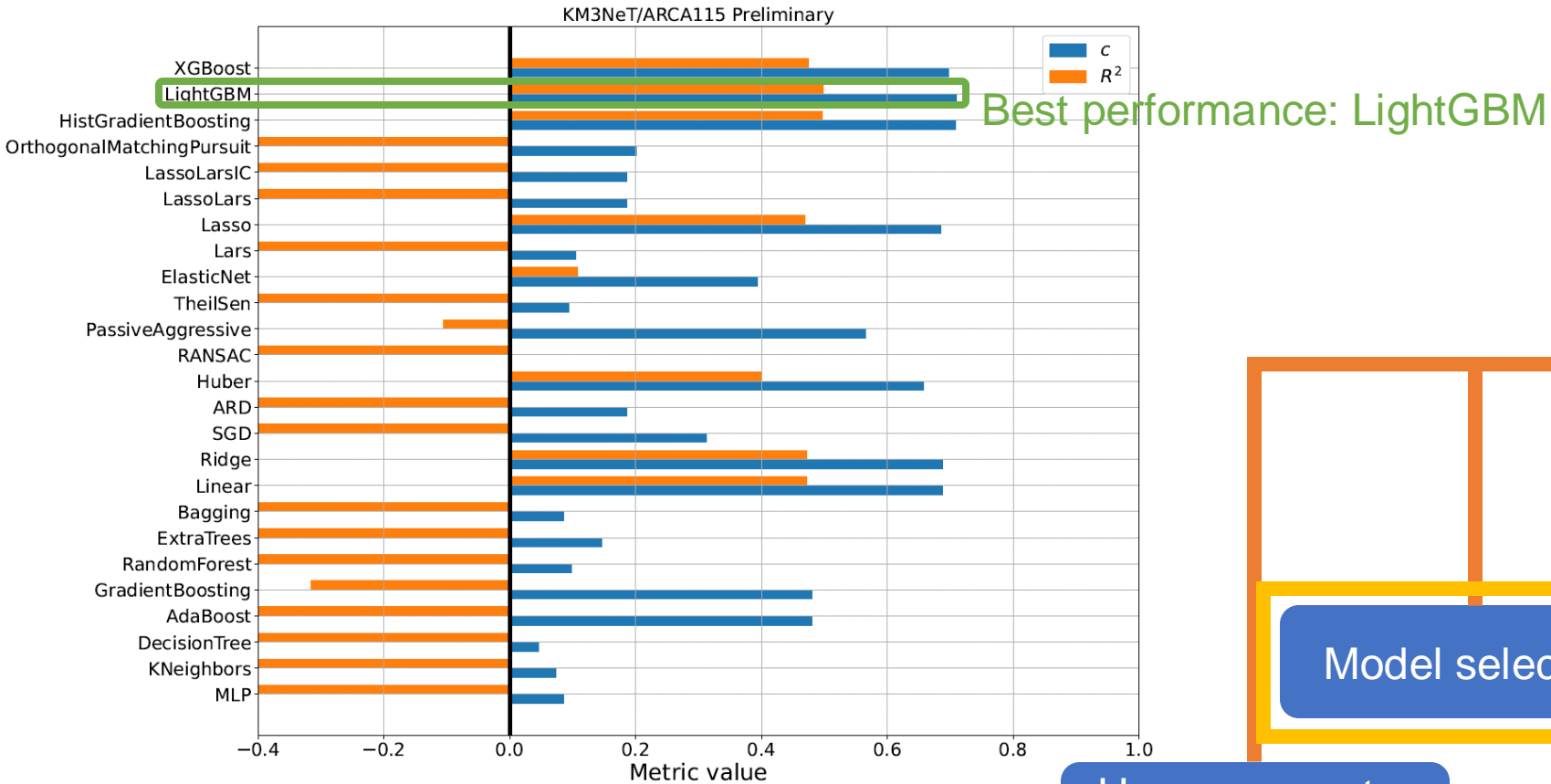






## Performance comparison

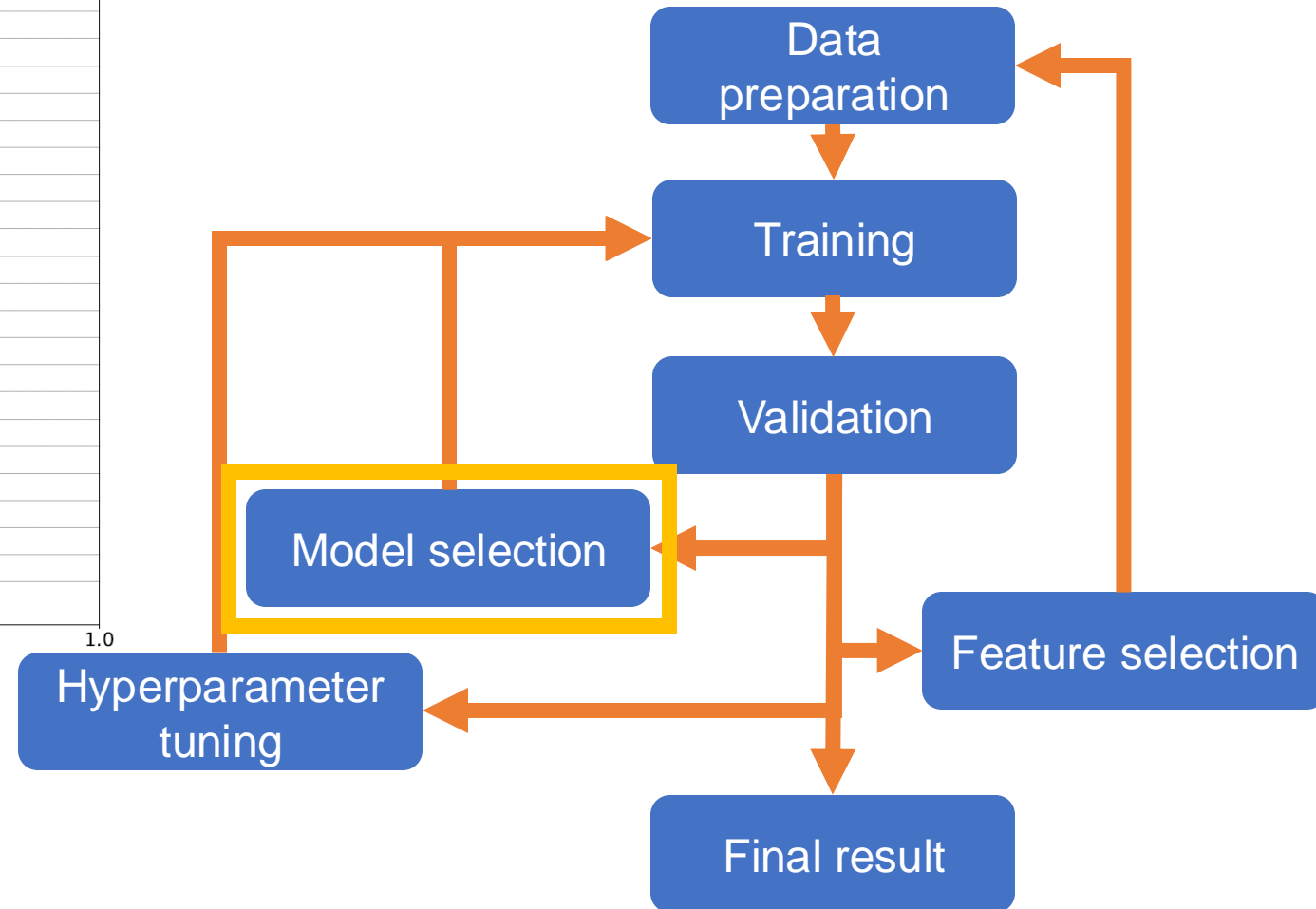
(on a fraction (50k events) of the training dataset):



Metrics:

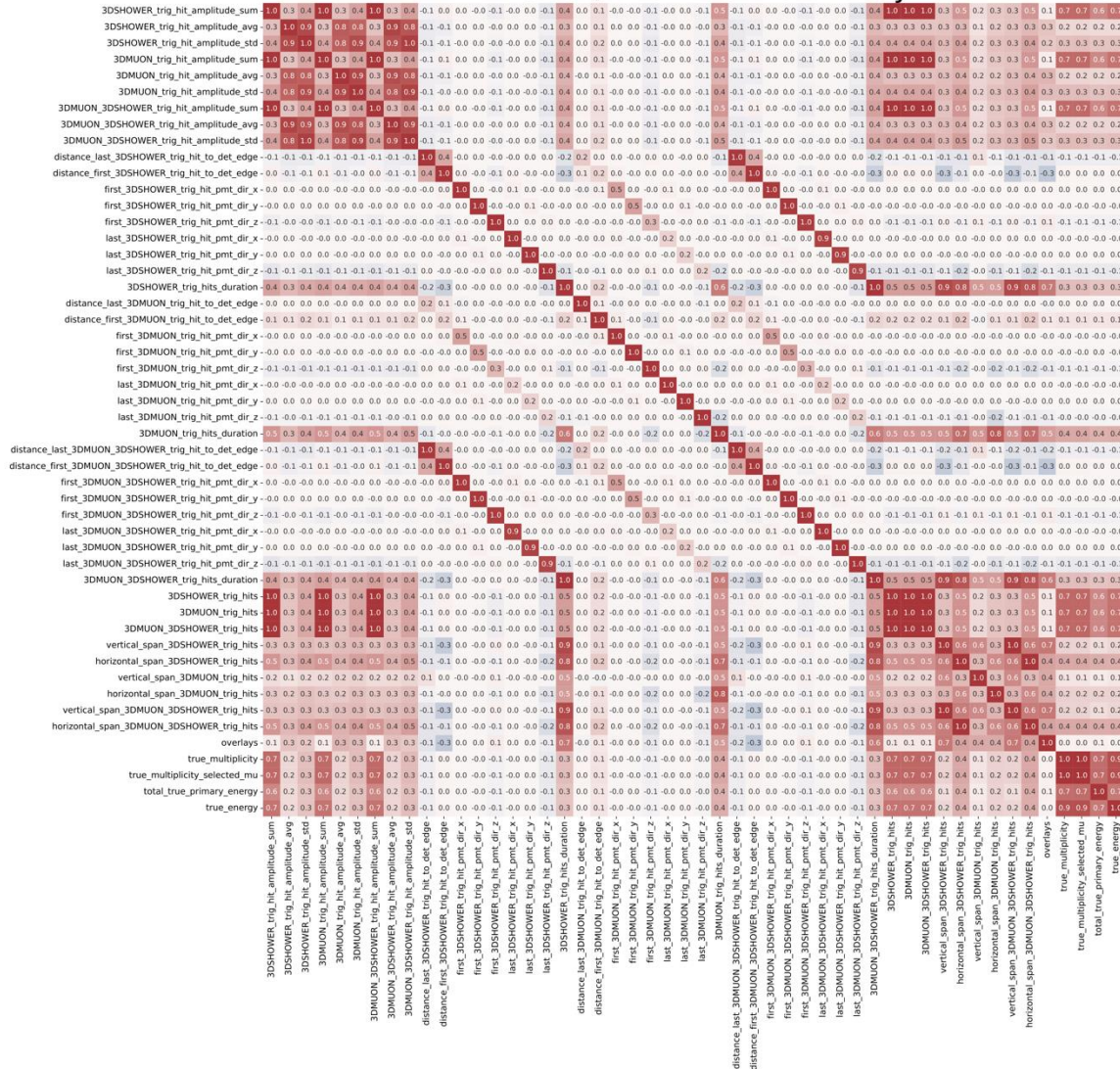
- ❖ weighted  $R^2$ -score
- ❖ weighted Pearson correlation coefficient

My workflow:



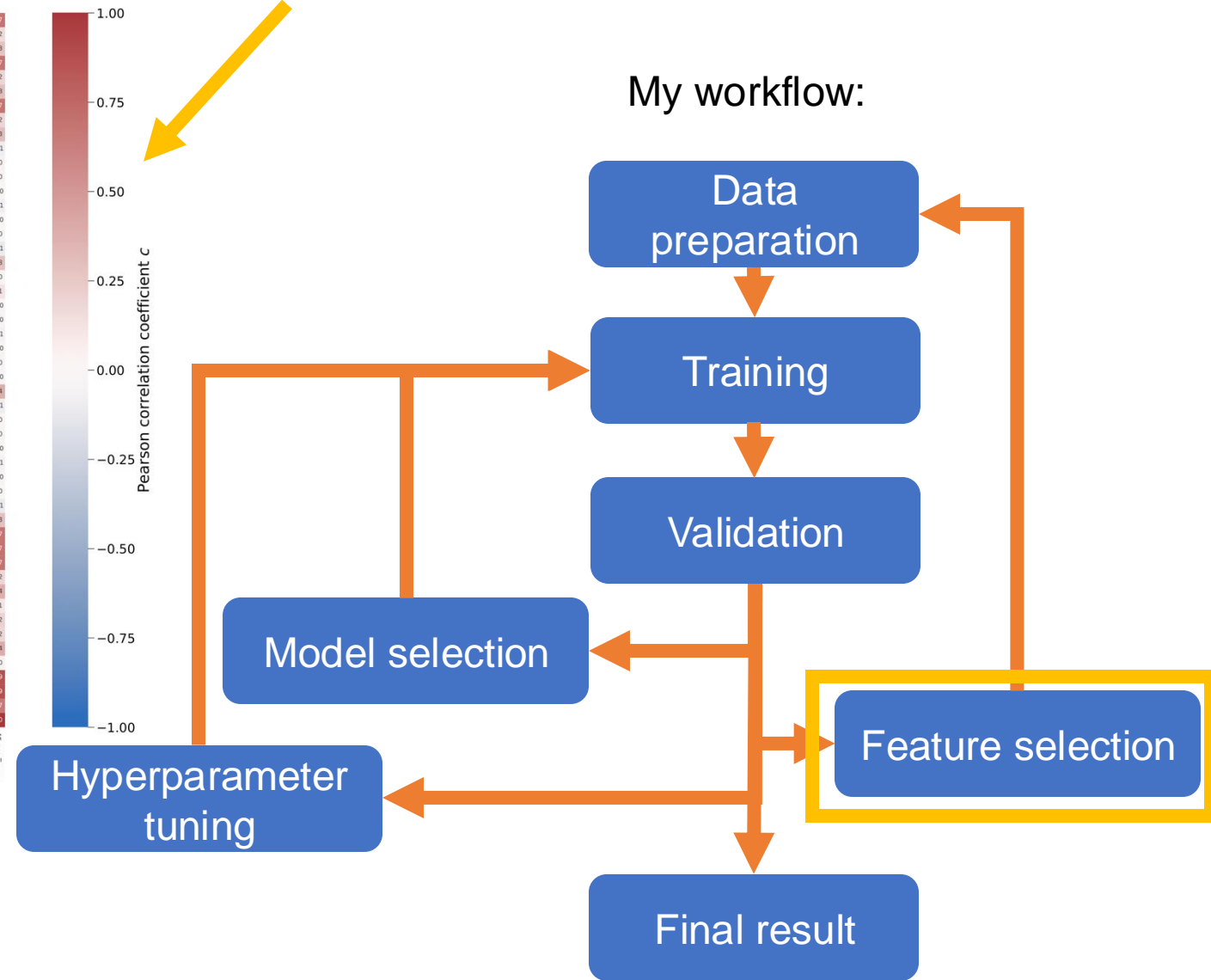
Correlation matrix of all 46 features and 4 targets:

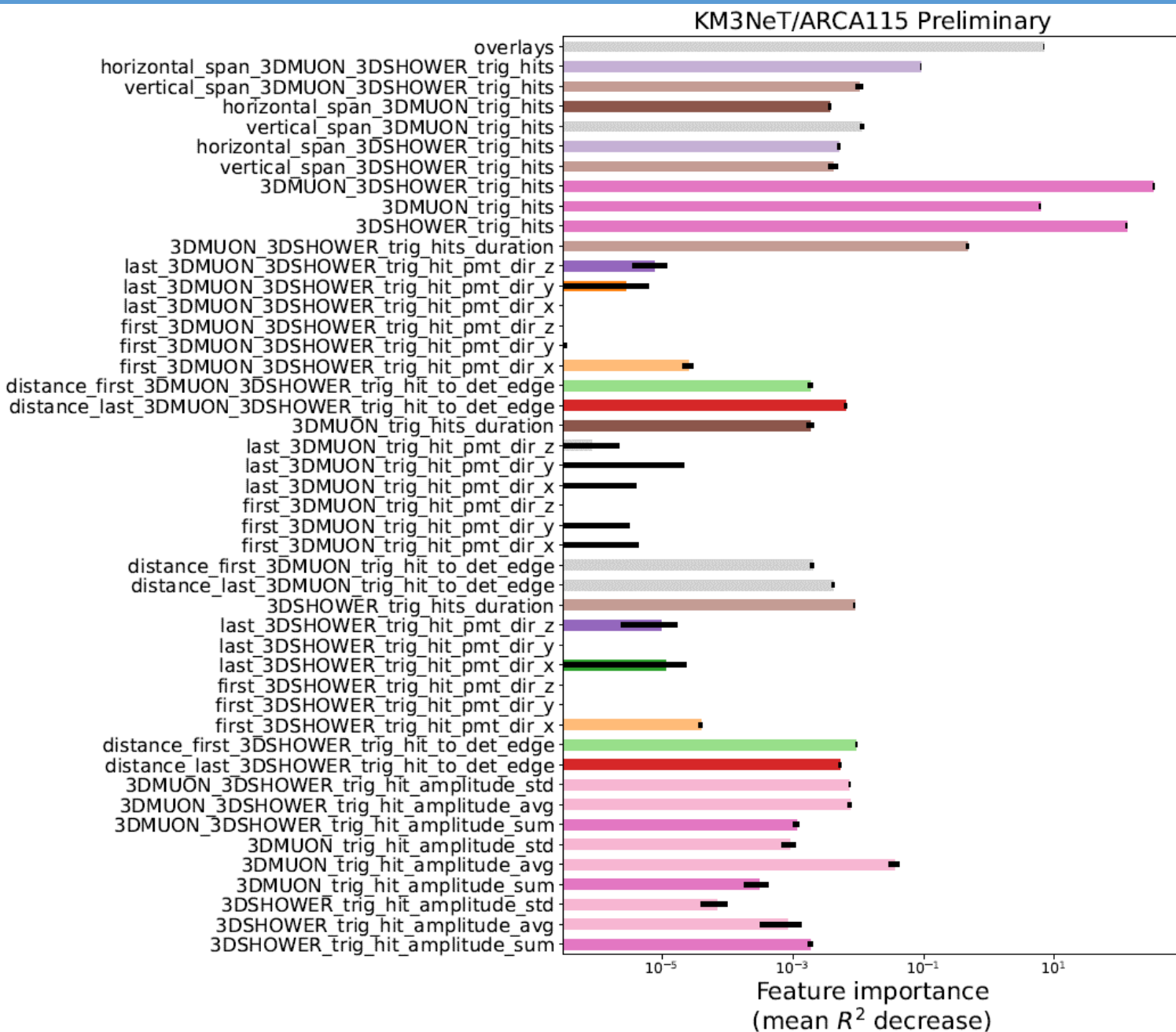
KM3Net/ARCA115 Preliminary



NOT equally important, maybe not all needed?

My workflow:





Colors not random!

They match the feature clustering (see backup)

The idea:

Try to select only the most important feature in each cluster?

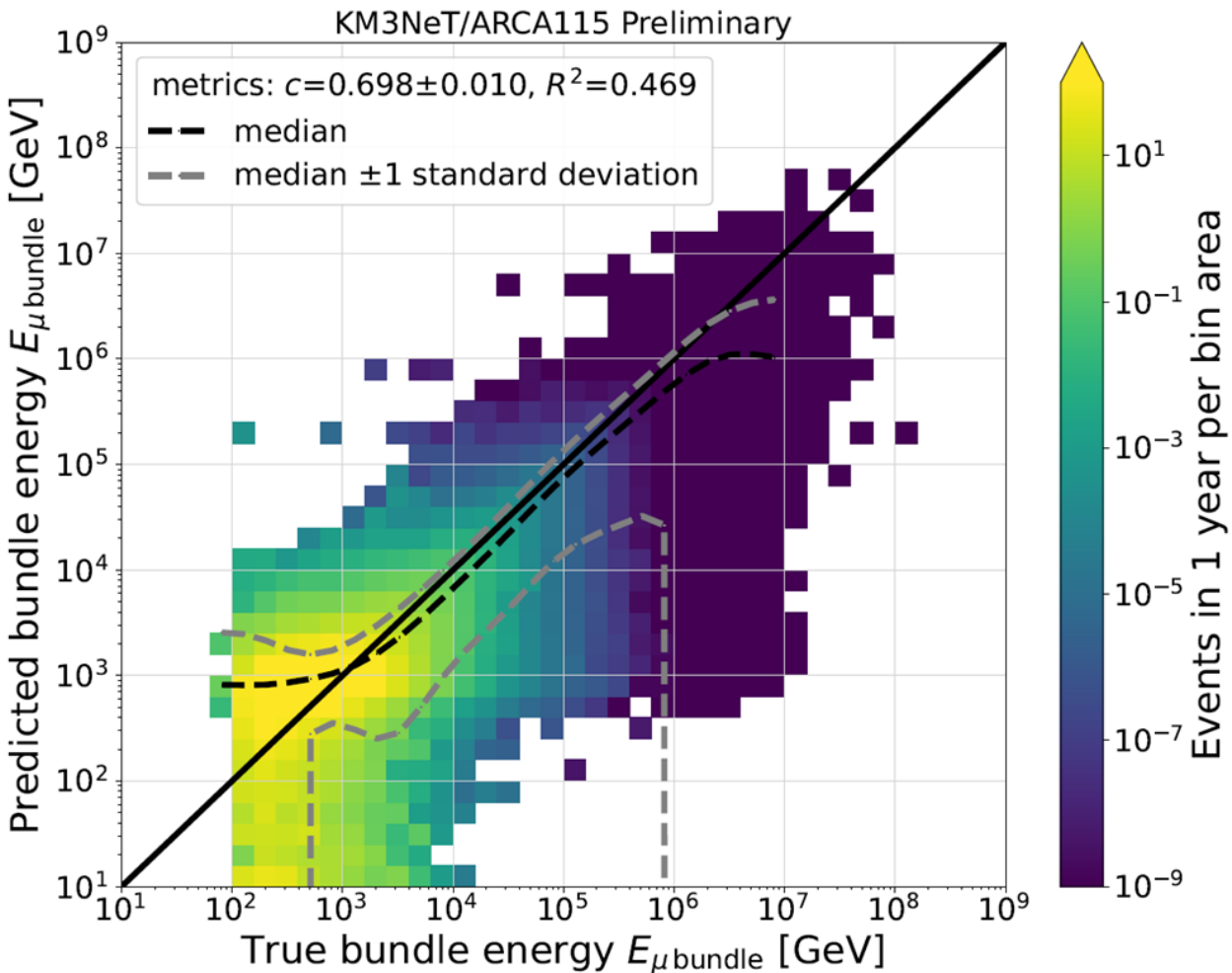
Feature	Importance
3DMUON_3DSHOWER_trig_hits	325
overlays	6.84
3DMUON_3DSHOWER_trig_hits_duration	0.47
horizontal_span_3DMUON_3DSHOWER_trig_hits	0.0900
3DMUON_trig_hit_amplitude_avg	0.0359
vertical_span_3DMUON_trig_hits	0.0114
distance_first_3DSHOWER_trig_hit_to_det_edge	0.0093
distance_last_3DMUON_3DSHOWER_trig_hit_to_det_edge	0.0063
distance_last_3DMUON_trig_hit_to_det_edge	0.0041
horizontal_span_3DMUON_trig_hits	0.0036
distance_first_3DMUON_trig_hit_to_det_edge	0.0020



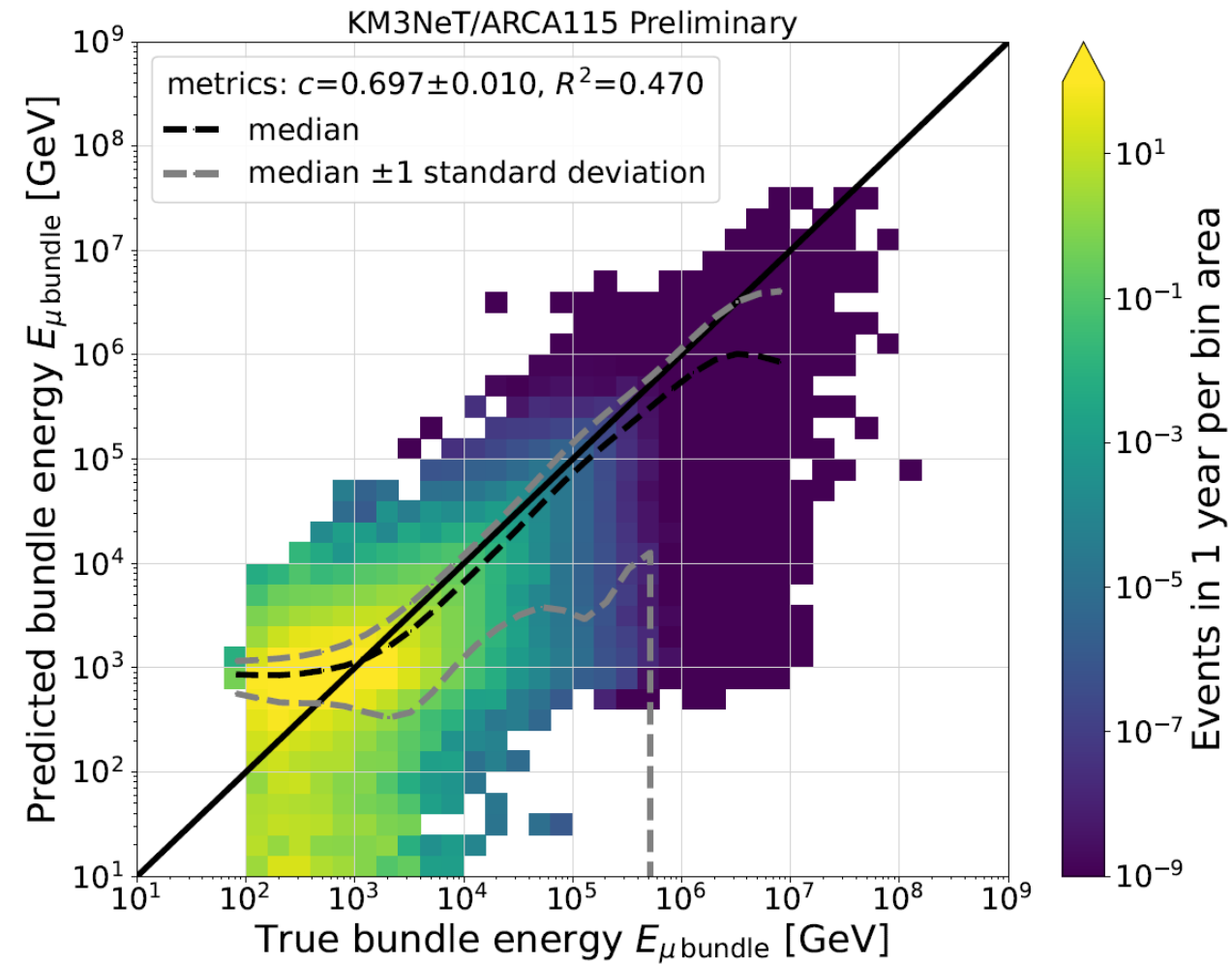
I considered 4 options:

1. All features
2. Features with importance>0 & only one per cluster
3. The most important feature only
4. Features with importance>0

## 1. All features



## 2. importance>0 & clustering

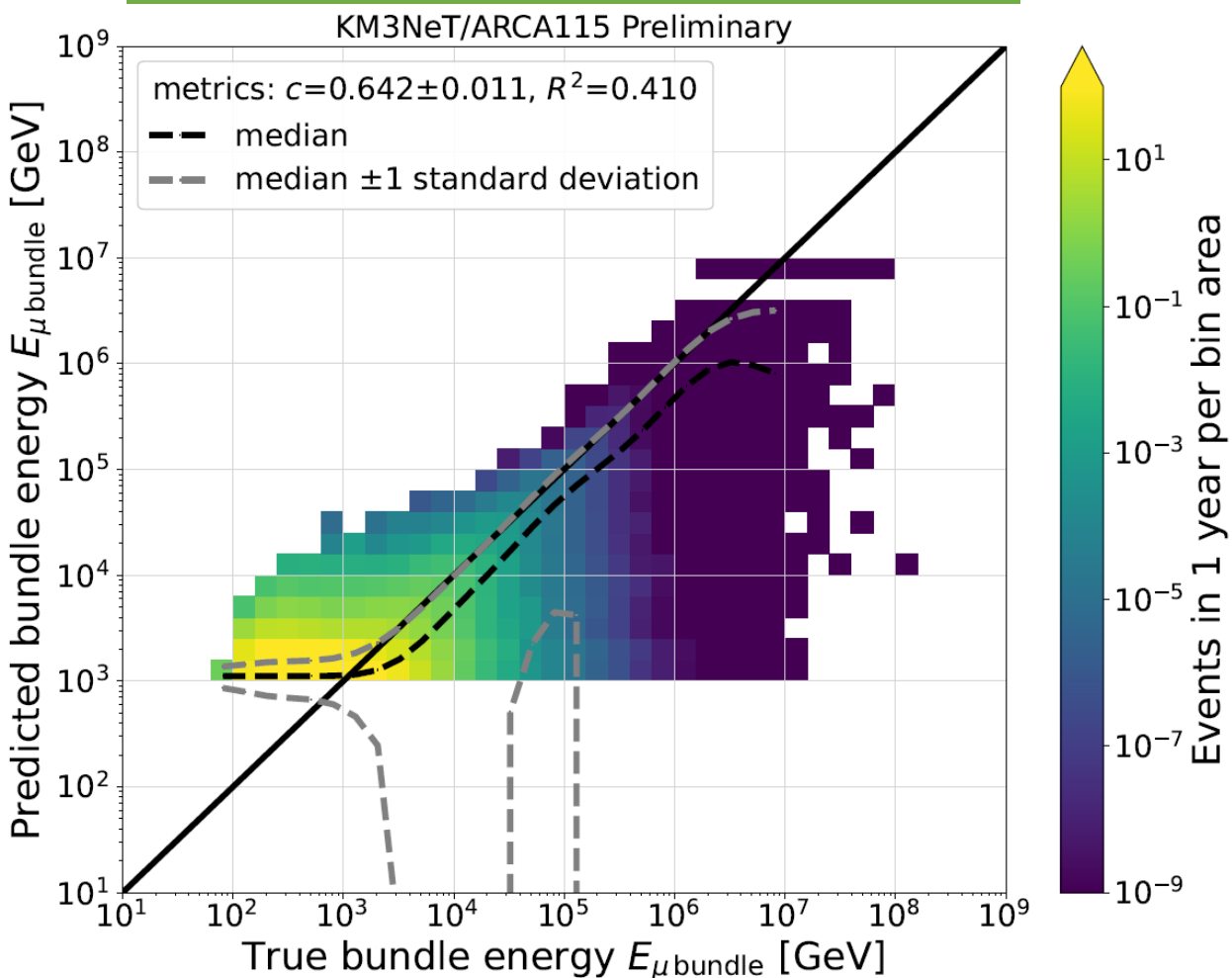


I considered 4 options:

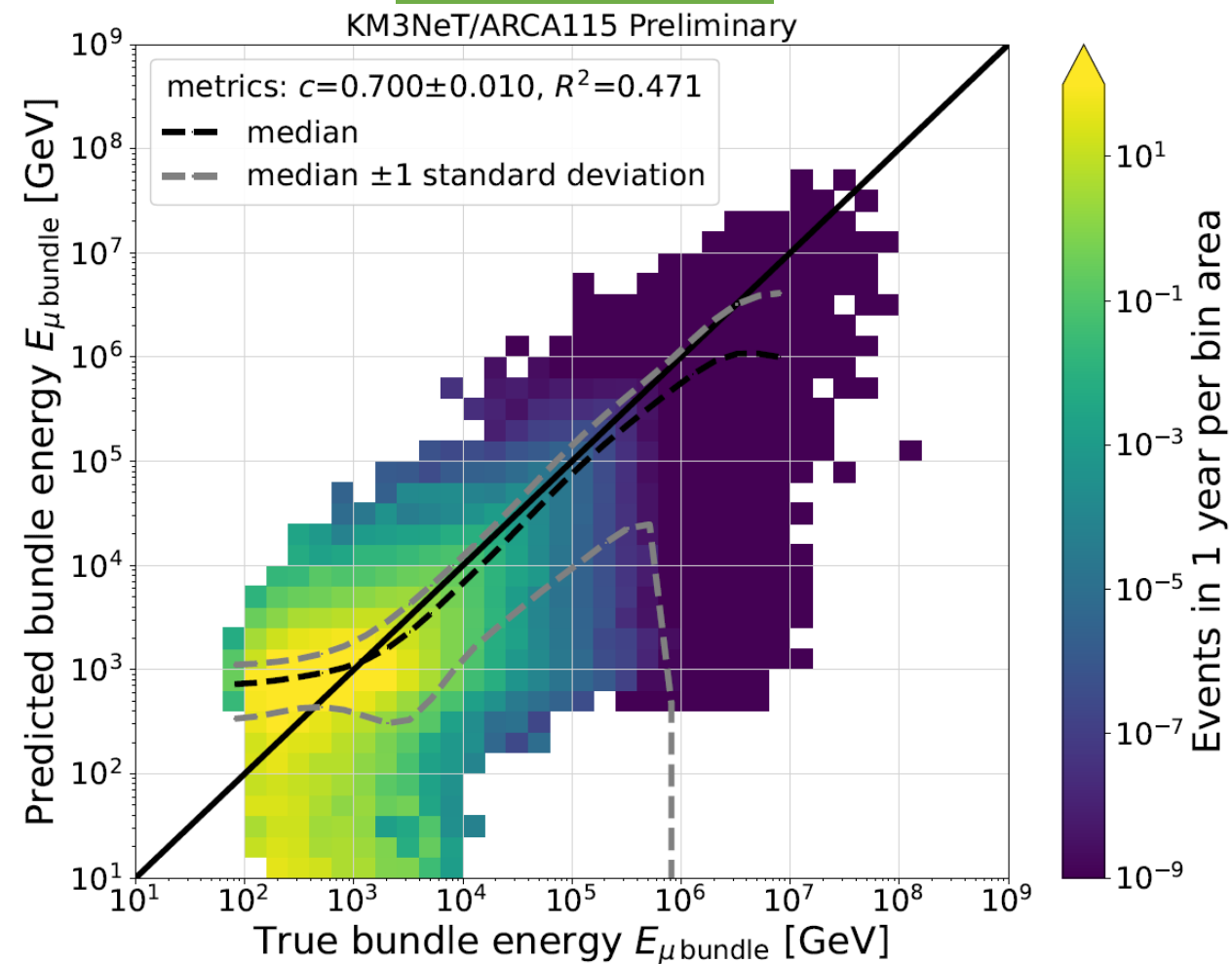
1. All features
2. Features with importance>0 & only one per cluster

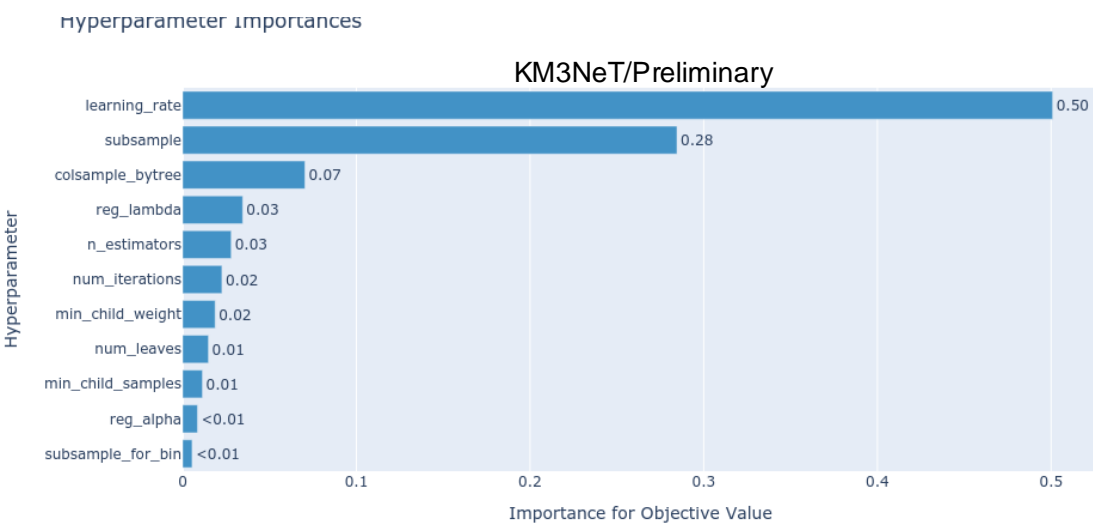
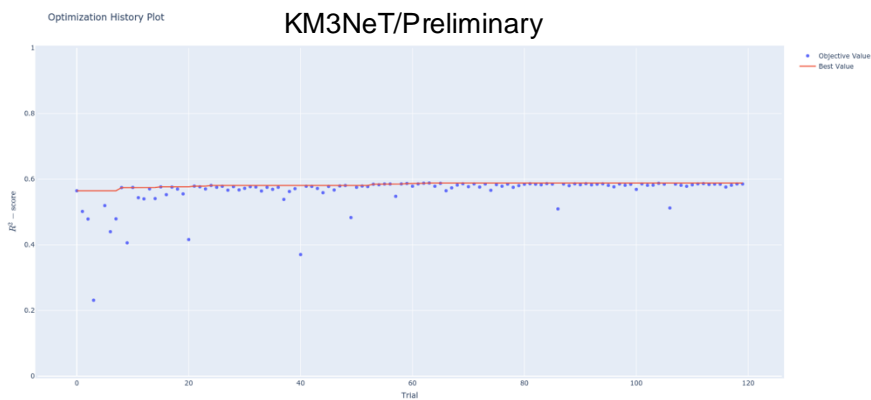
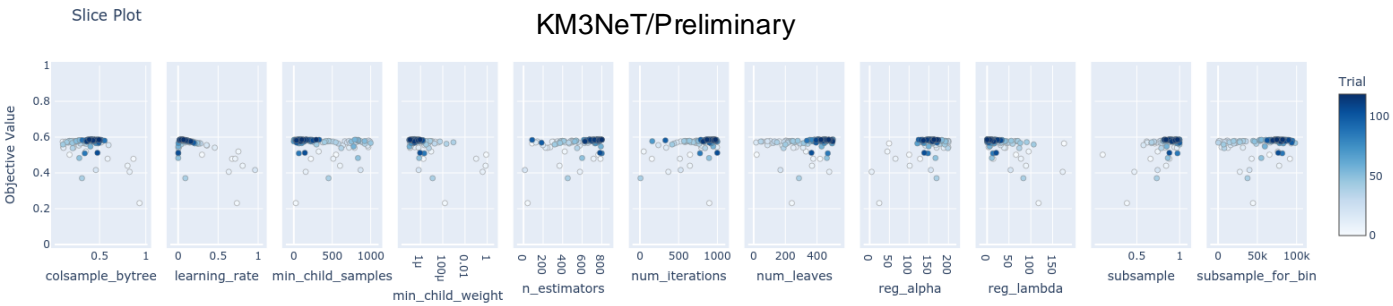
3. The most important feature only
4. Features with importance>0

## 3. 3DMUON\_3DSHOWER\_trig\_hits only

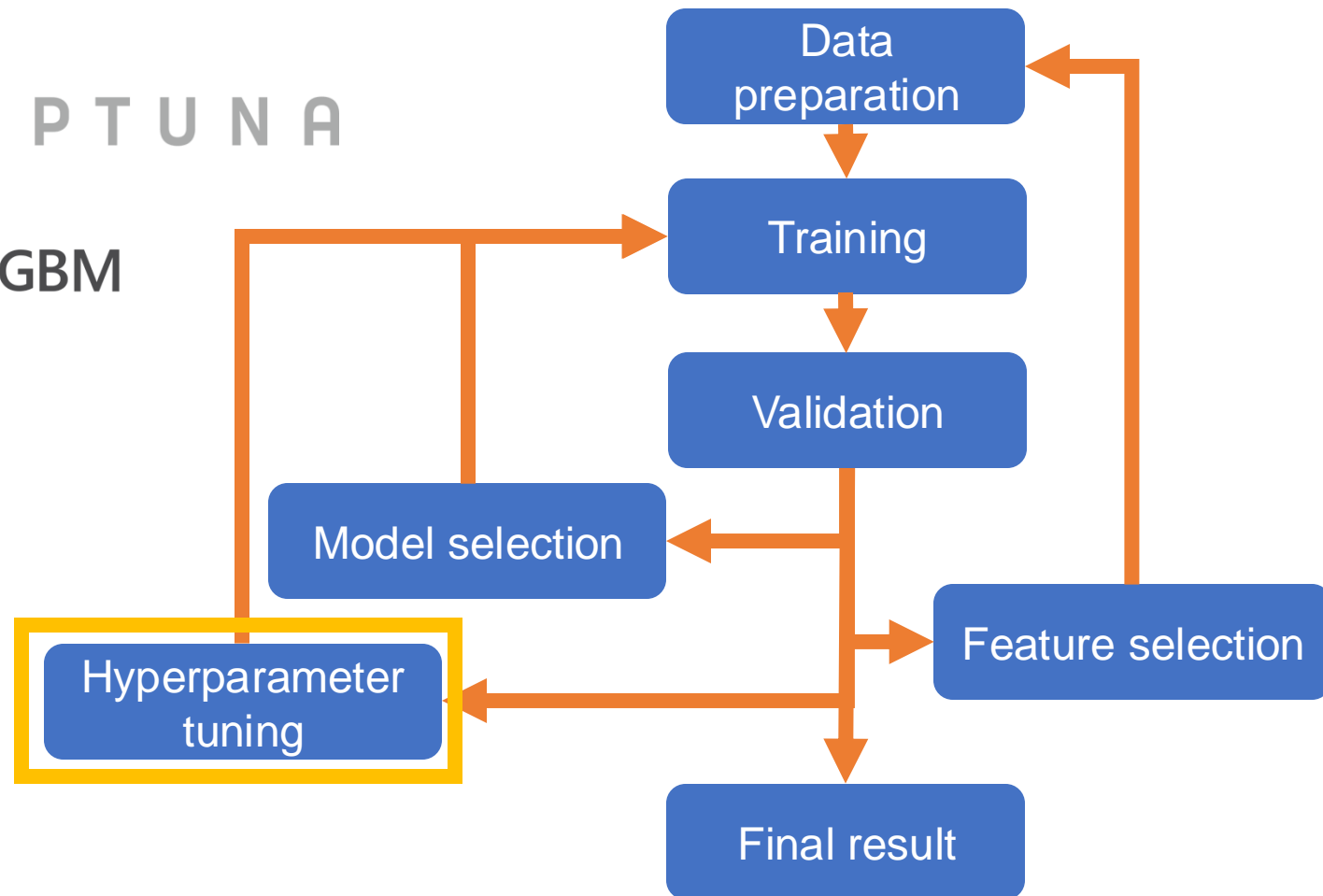


## 4. importance>0





My workflow:

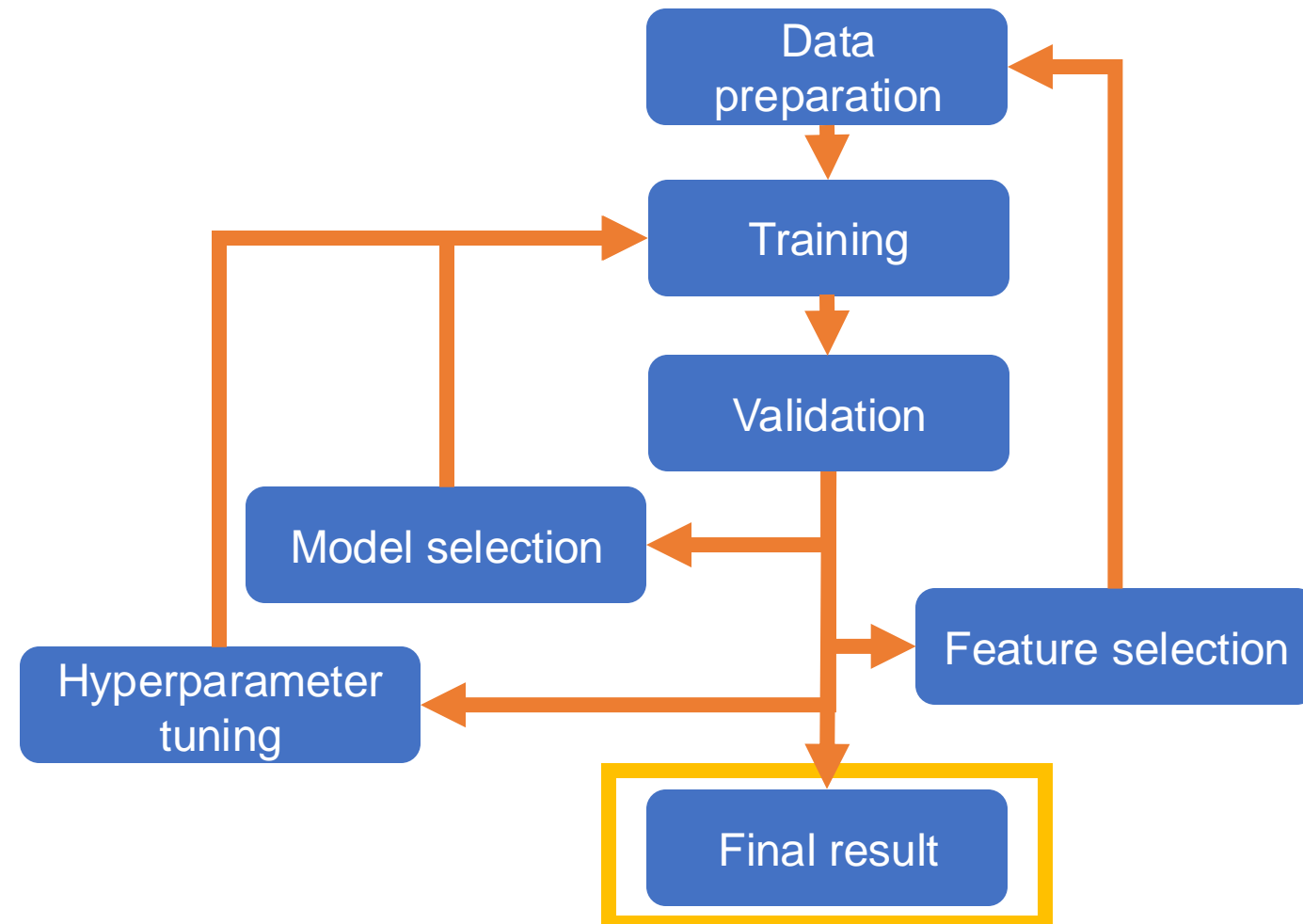




Note:

I show only some of the results!  
(because there is too much)

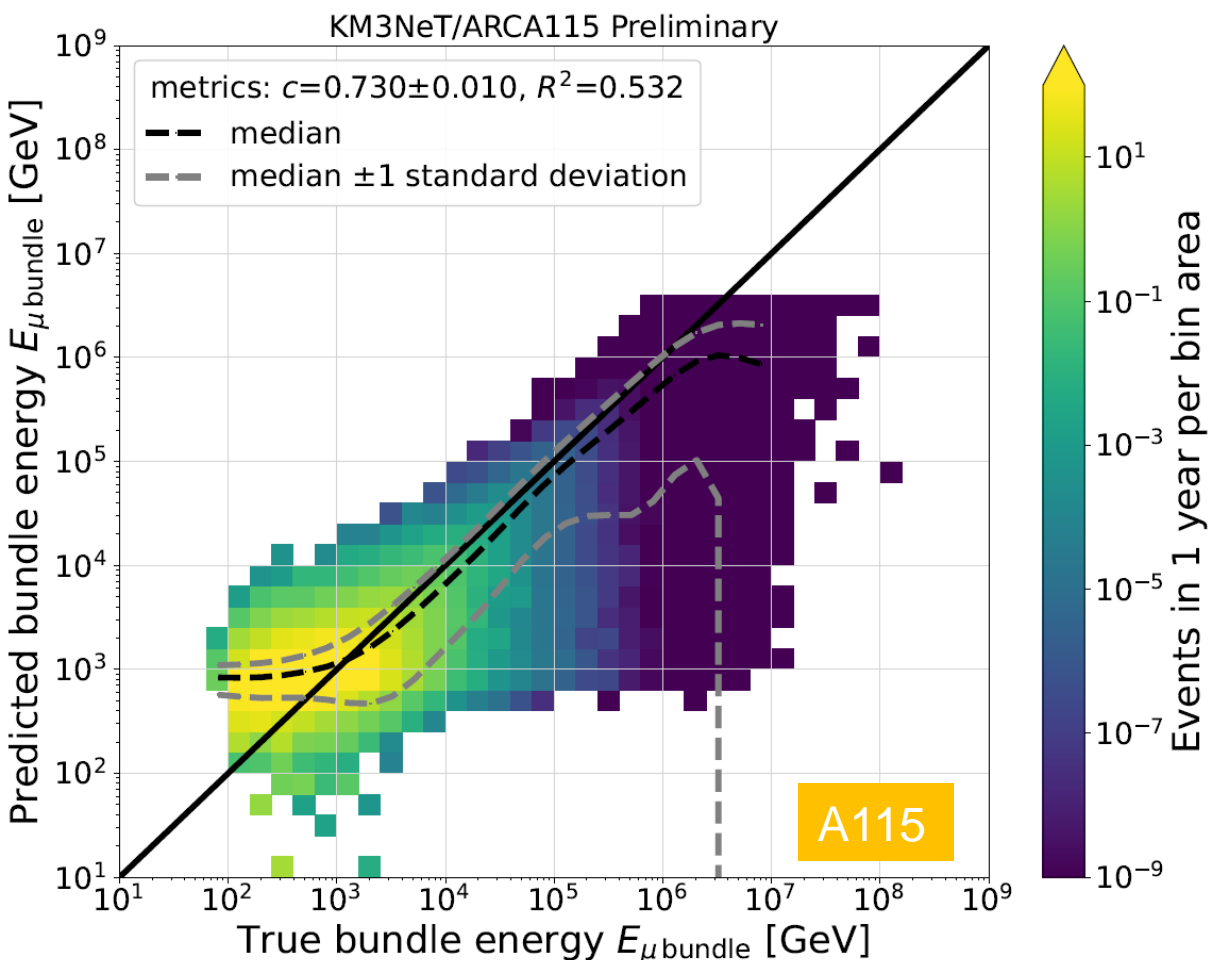
My workflow:



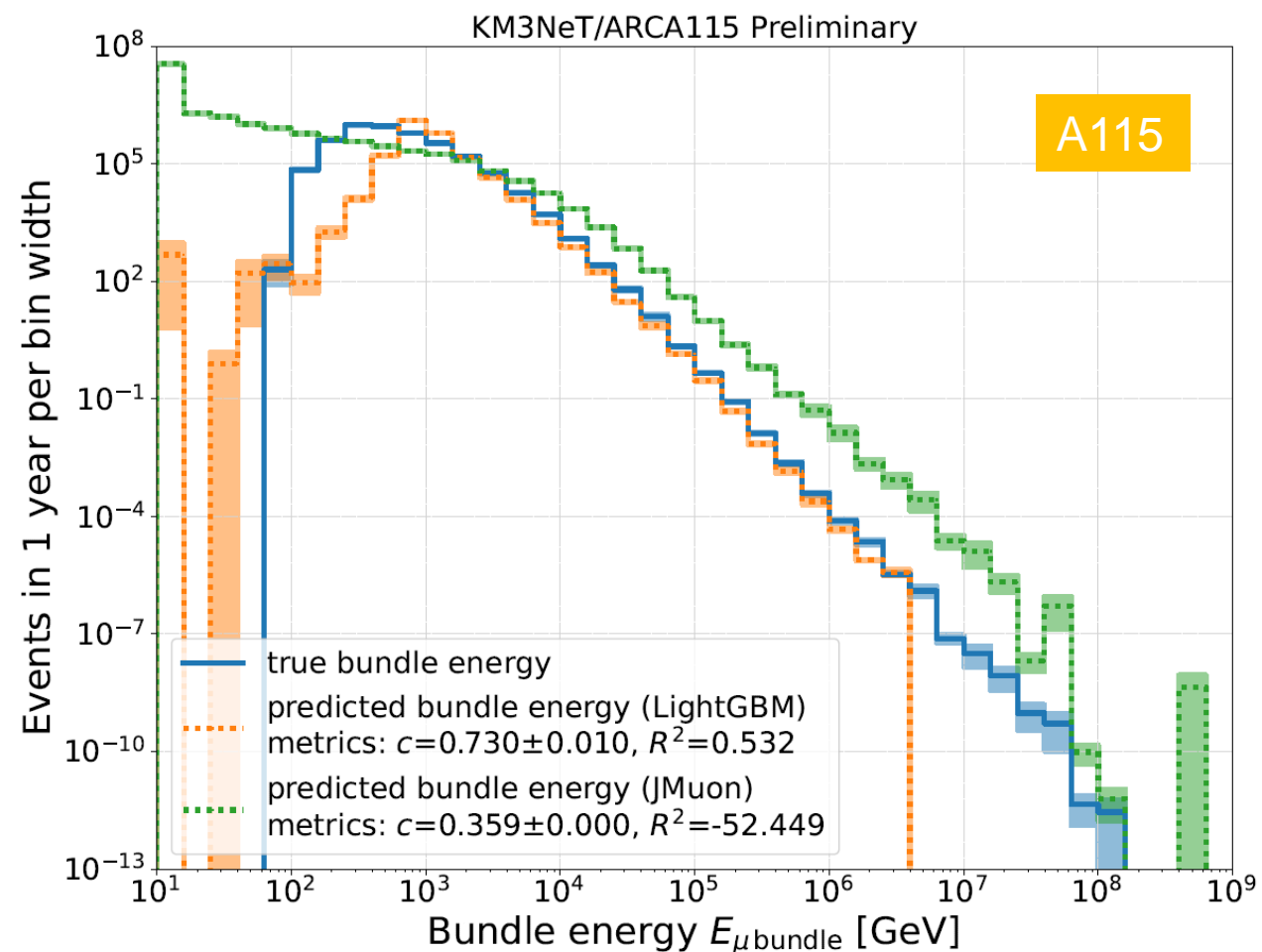
Analogous results for ARCA6,  
ORCA115 and ORCA6

## Results for ARCA115:

2D: reco vs true



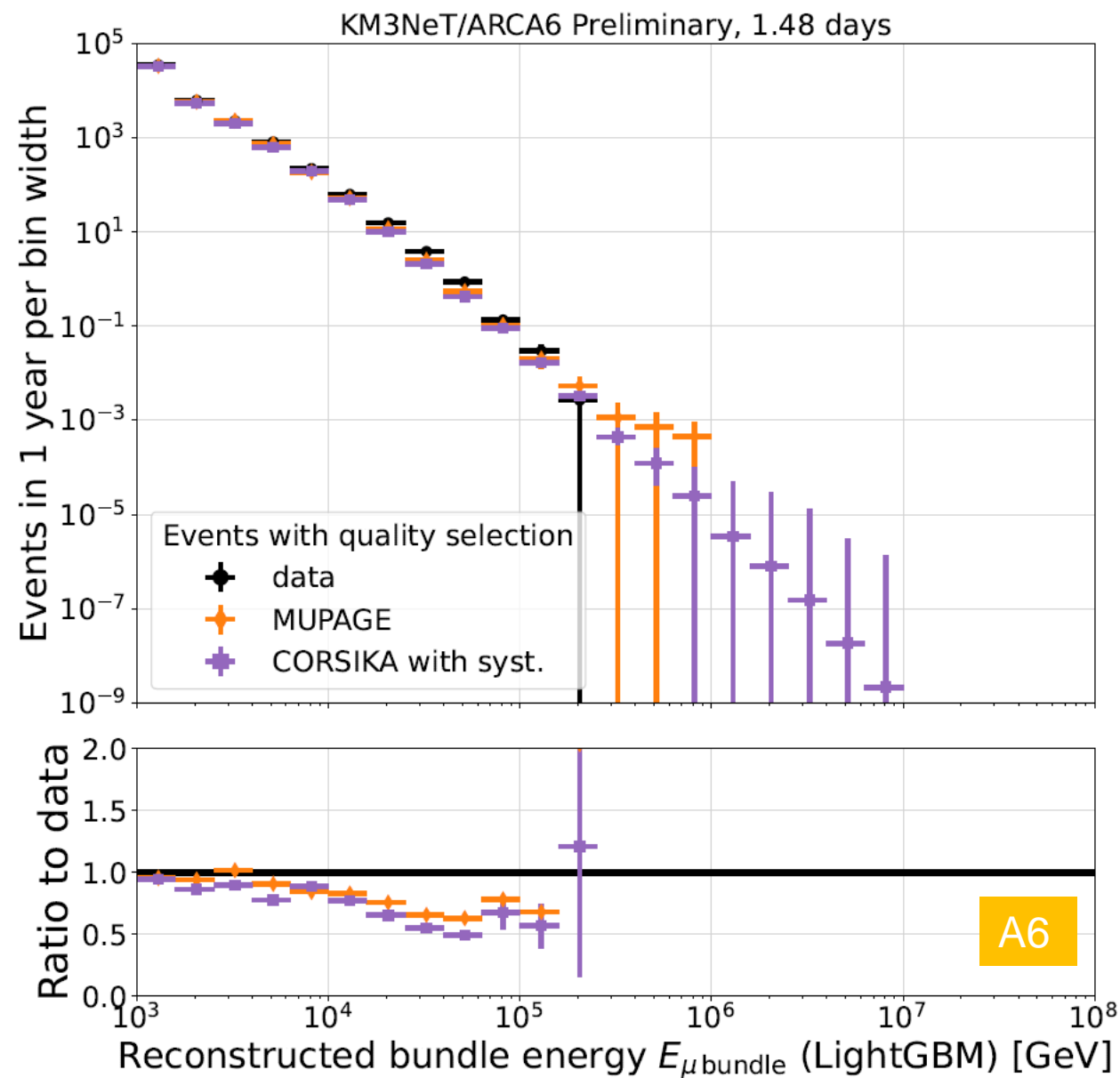
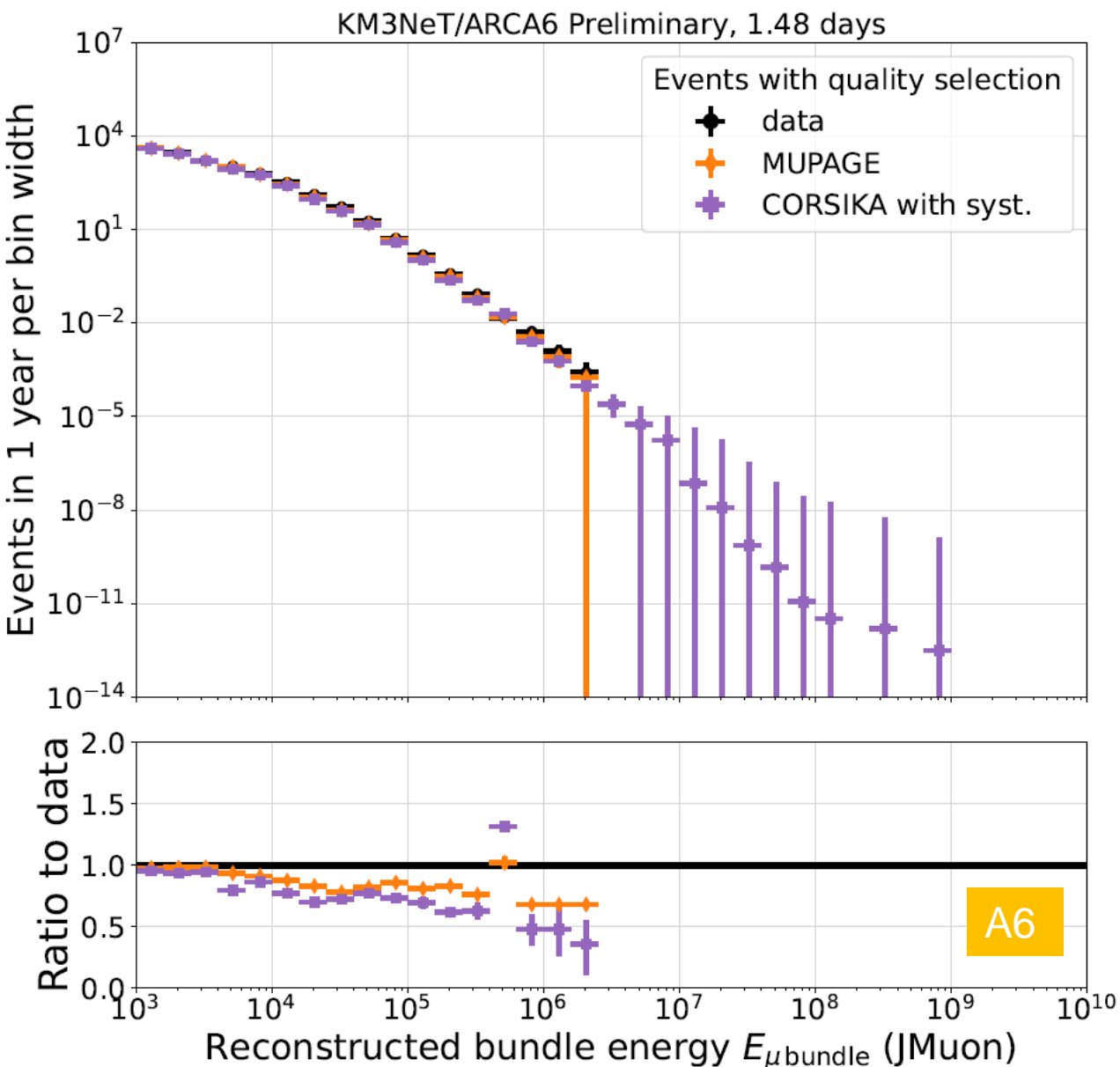
1D histograms



Jmuon (standard reco)

Analogous results for ORCA6

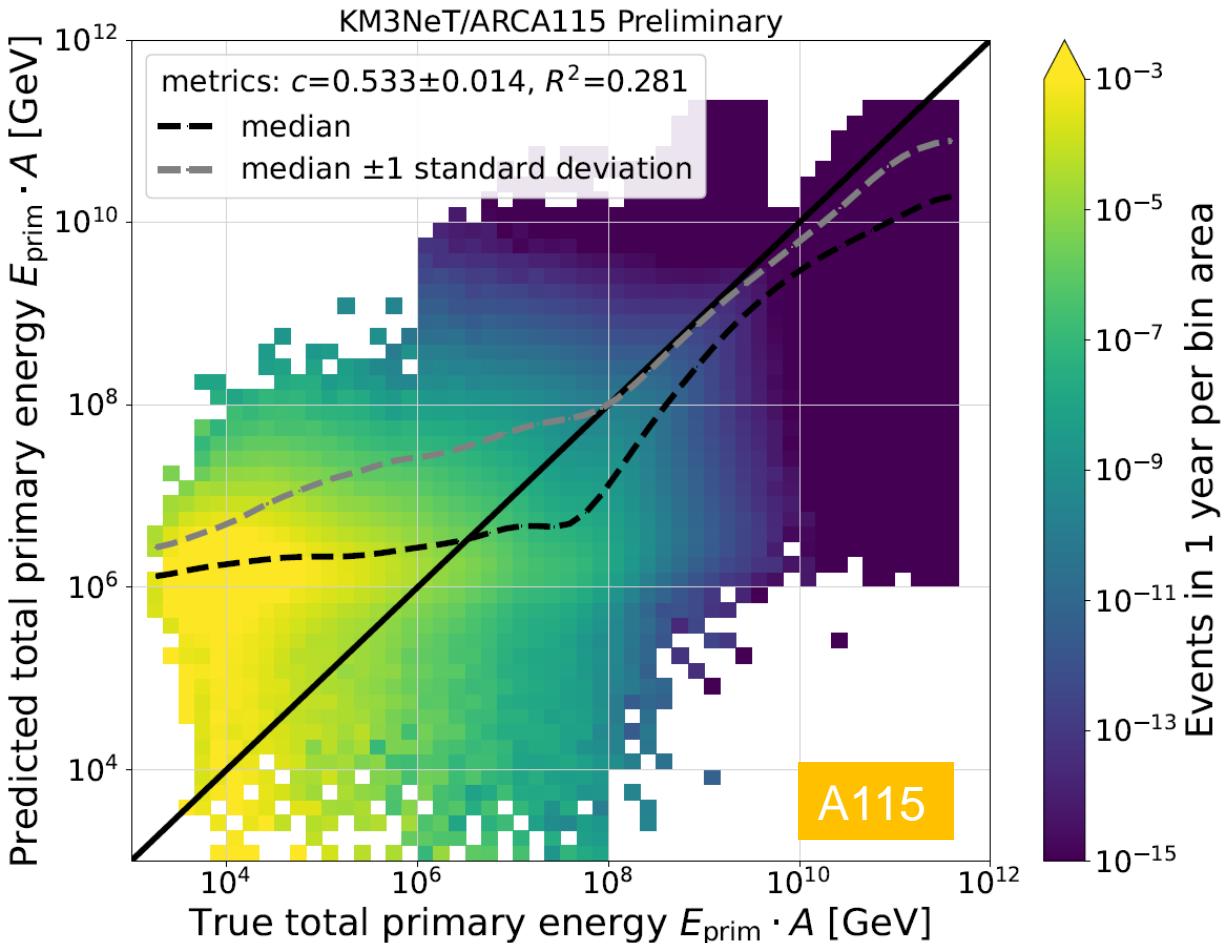
LightGBM



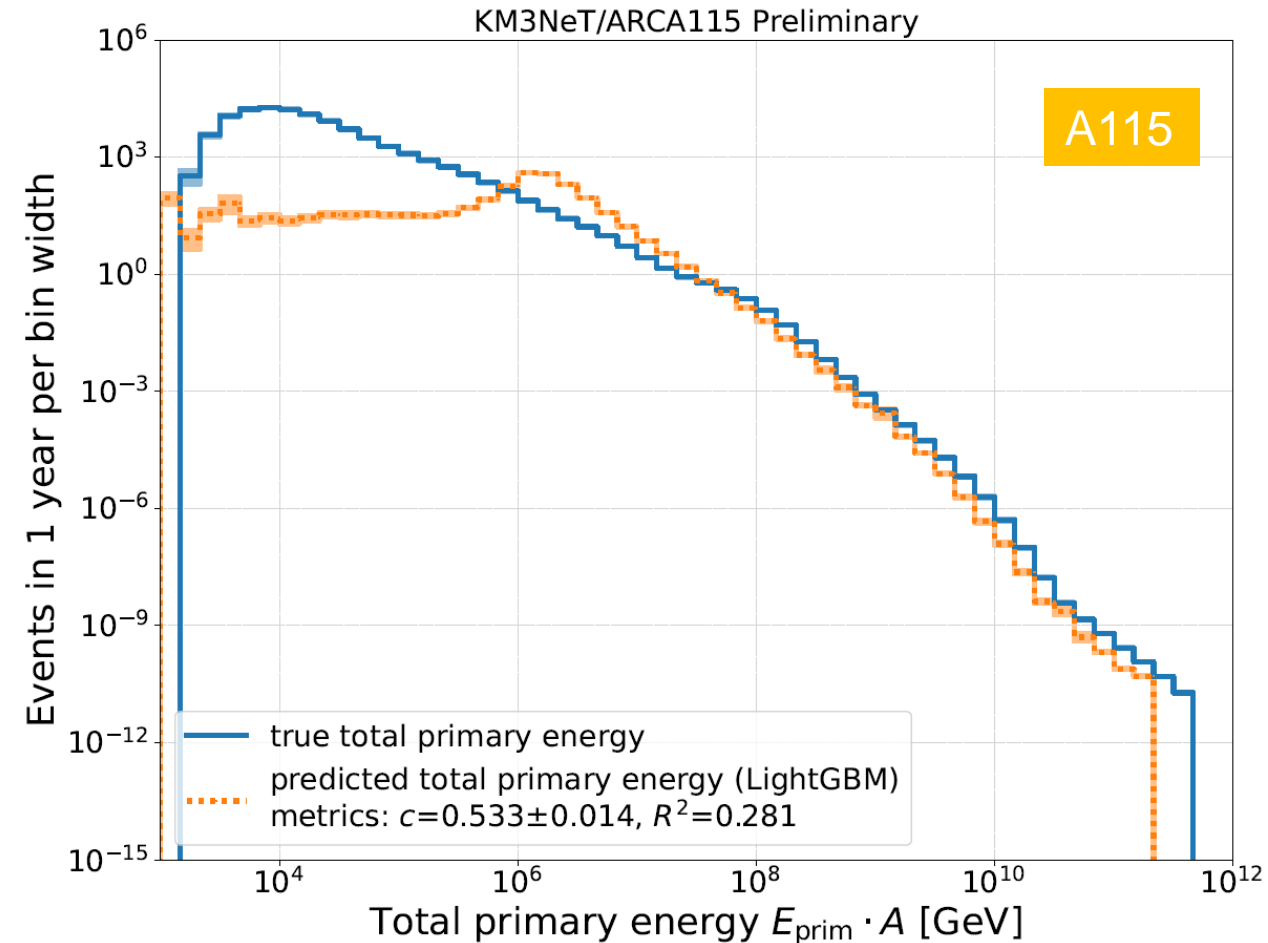
## Results for ARCA115:

Analogous results for ARCA6,  
ORCA115 and ORCA6

2D: reco vs true

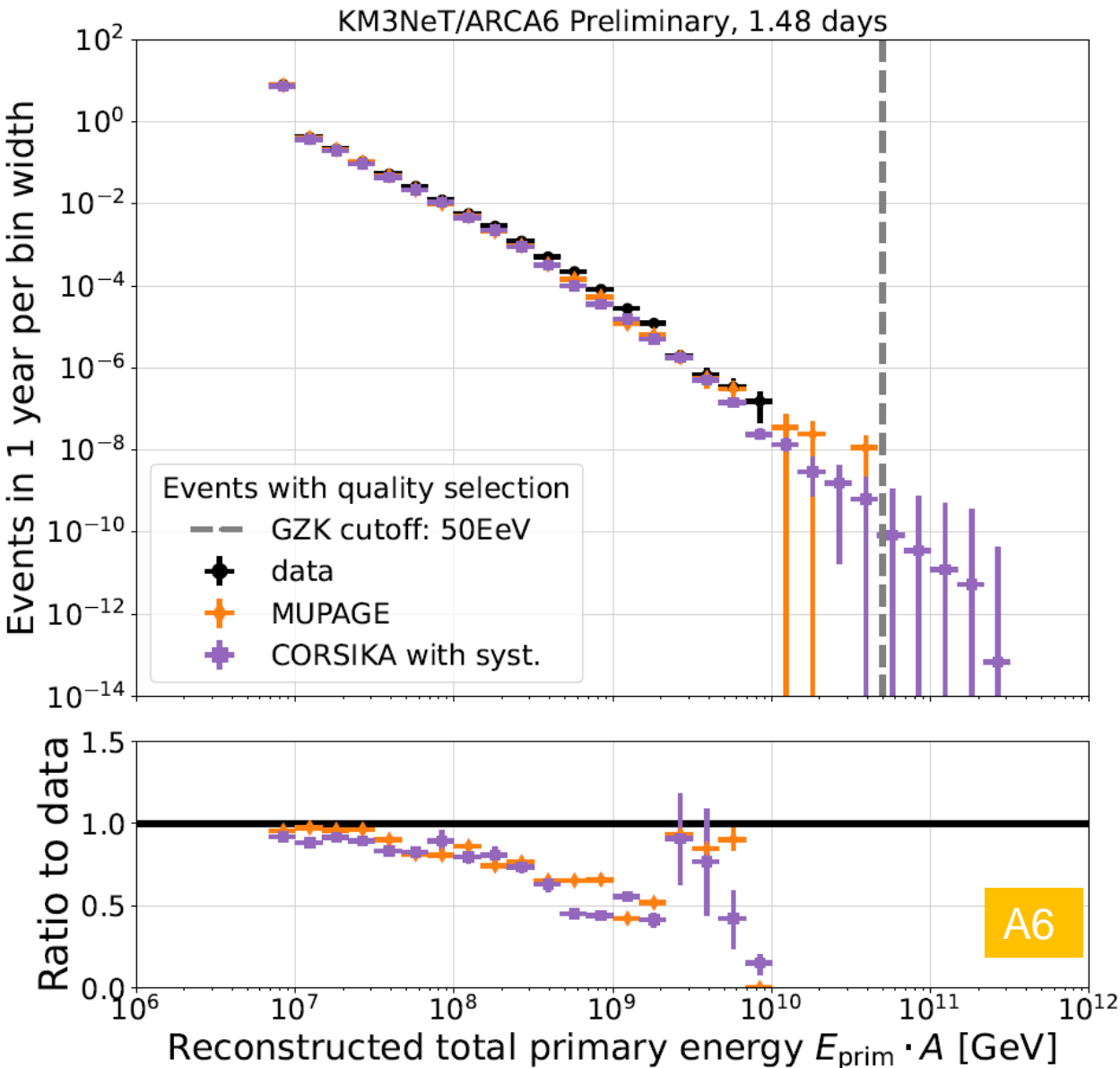


1D histograms



LightGBM

Analogous results for ORCA6



Results obtained with ARCA6/ORCA6:

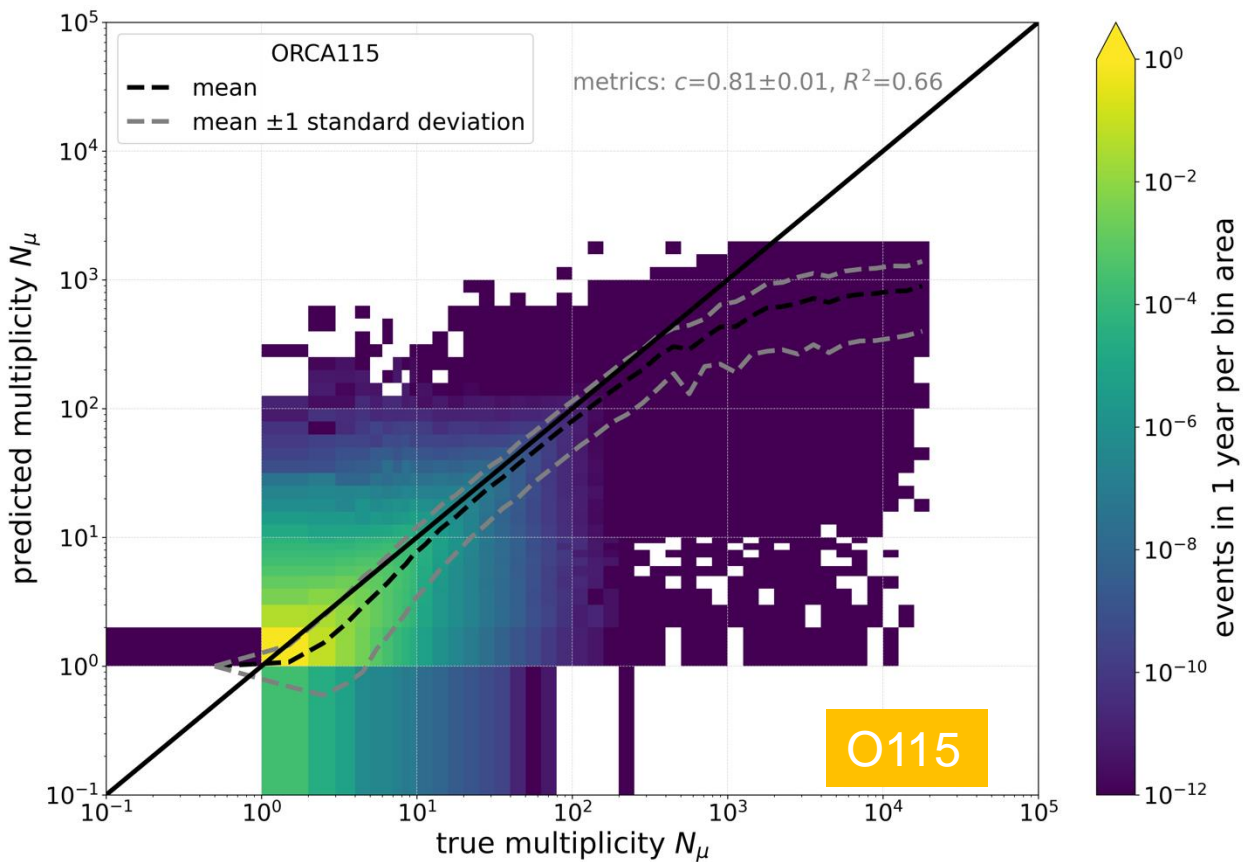
- ❖ First measurement of primary CR energy with KM3NeT detectors ever
- ❖ Simulations underestimate the flux at high energies (similarly as for bundle energy; expected)
- ❖ The Greisen–Zatsepin–Kuzmin (GZK) cutoff cannot be confirmed/excluded (yet!)

\*GZK cutoff – theoretical upper bound on possible CR energy, due to interactions with the cosmic microwave background radiation (CMB)

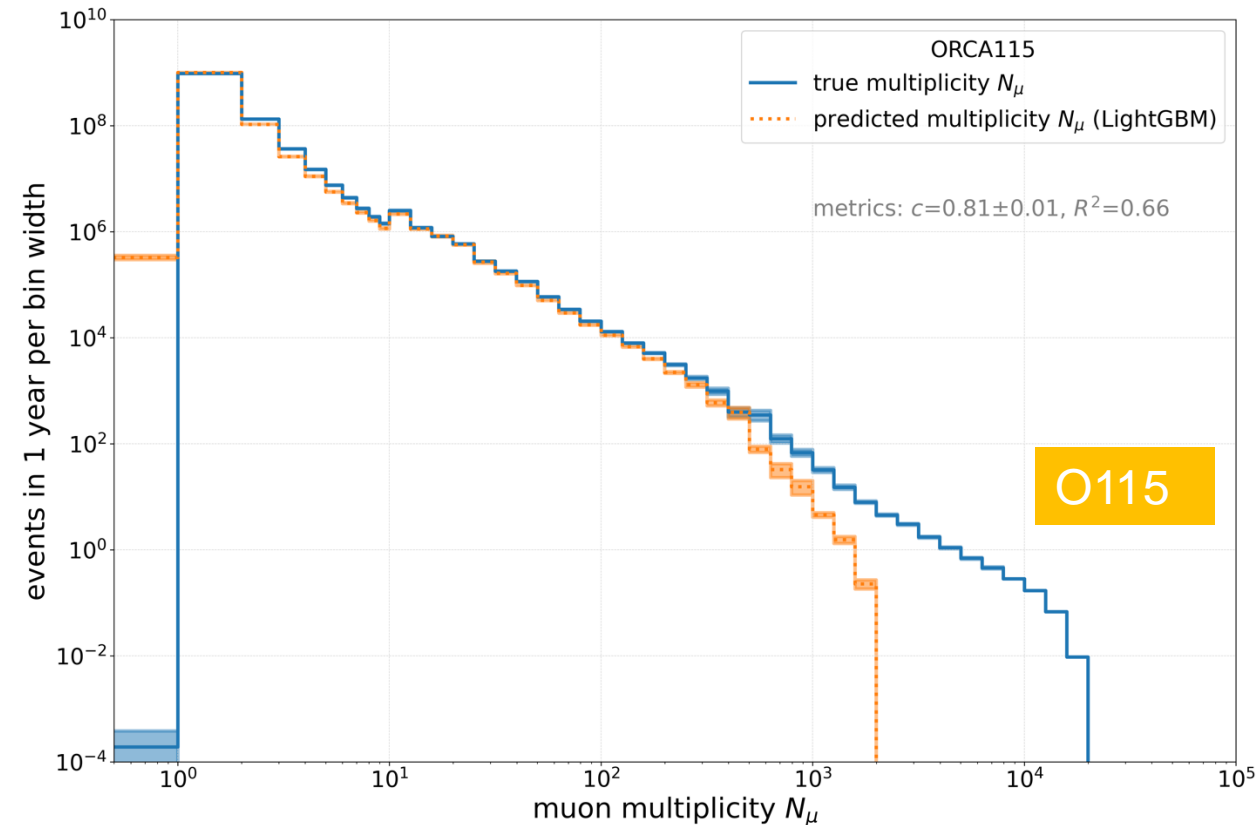
Analogous results for ARCA6,  
ARCA115 and ORCA6

## Results for ORCA115:

2D: reco vs true

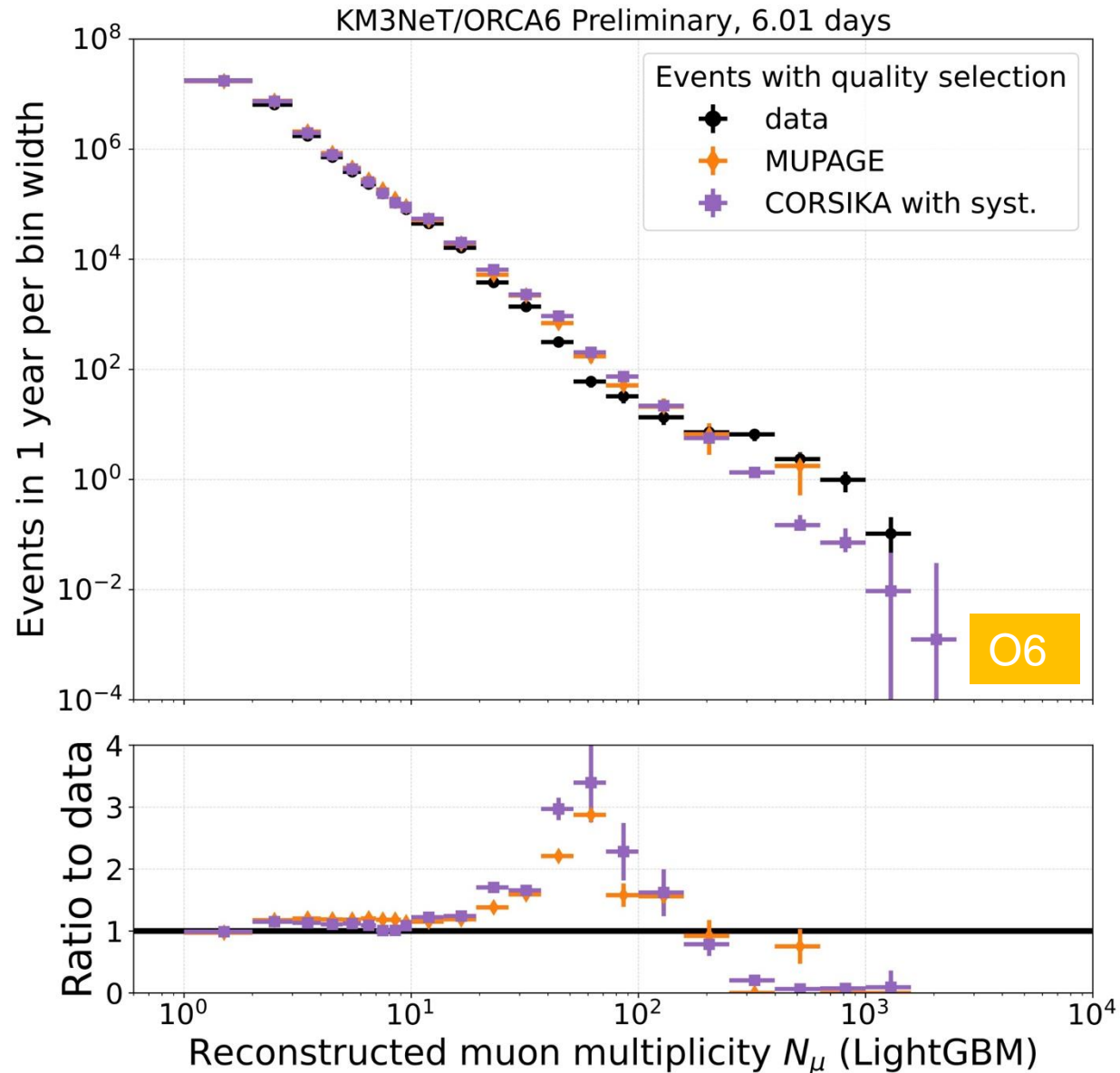


1D histograms



LightGBM

Analogous results for ARCA6



Results obtained with ARCA6/ORCA6 data:

- ❖ First muon multiplicity measurement in KM3NeT:
  - Ex aequo with S. Reck (using ORCA4 data)
  - First ever for ARCA
- ❖ Mid-multiplicities overestimated in simulations
- ❖ High multiplicities underestimated in simulations



# Outline

Introduction



Muon event reconstruction



Summary

More in my Thesis: [arXiv:2402.02620v1](https://arxiv.org/abs/2402.02620v1)  
and upcoming gSeaGen paper ...

## Summary:

- ❖ KM3NeT detectors under construction, but already collecting valuable data
- ❖ Accurate muon simulations are crucial
- ❖ Reconstructing  $N_\mu$ ,  $E_{\text{bundle}}$ ,  $E_{\text{prim}}$  possible

## Outlook:

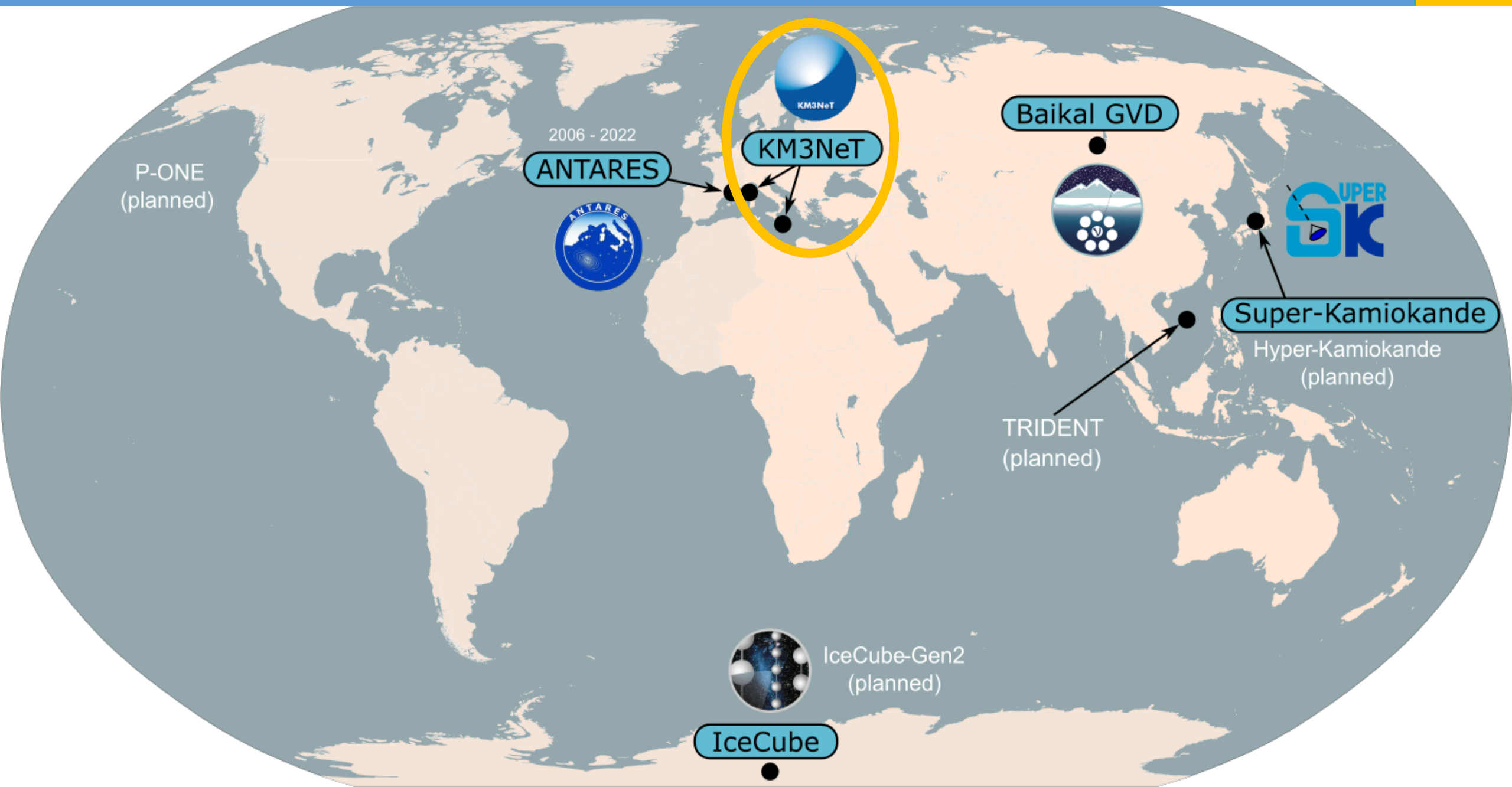
- ❖ Even lower level information as features?
- ❖ Reconstruction of individual muon tracks?



**Thank you for your attention!**



# Backup



## Digital Optical Module (DOM)

acrylic glass sphere with:

- 31 3" PMTs,
- readout electronics,
- pressure gauge,
- acoustic sensors,
- ...

2022 JINST 17 P0703

JATIS 7(1), 016001 (2021)

## Photomultiplier Tube (PMT)

converts light into electric signal

JINST13 (2018) P05035





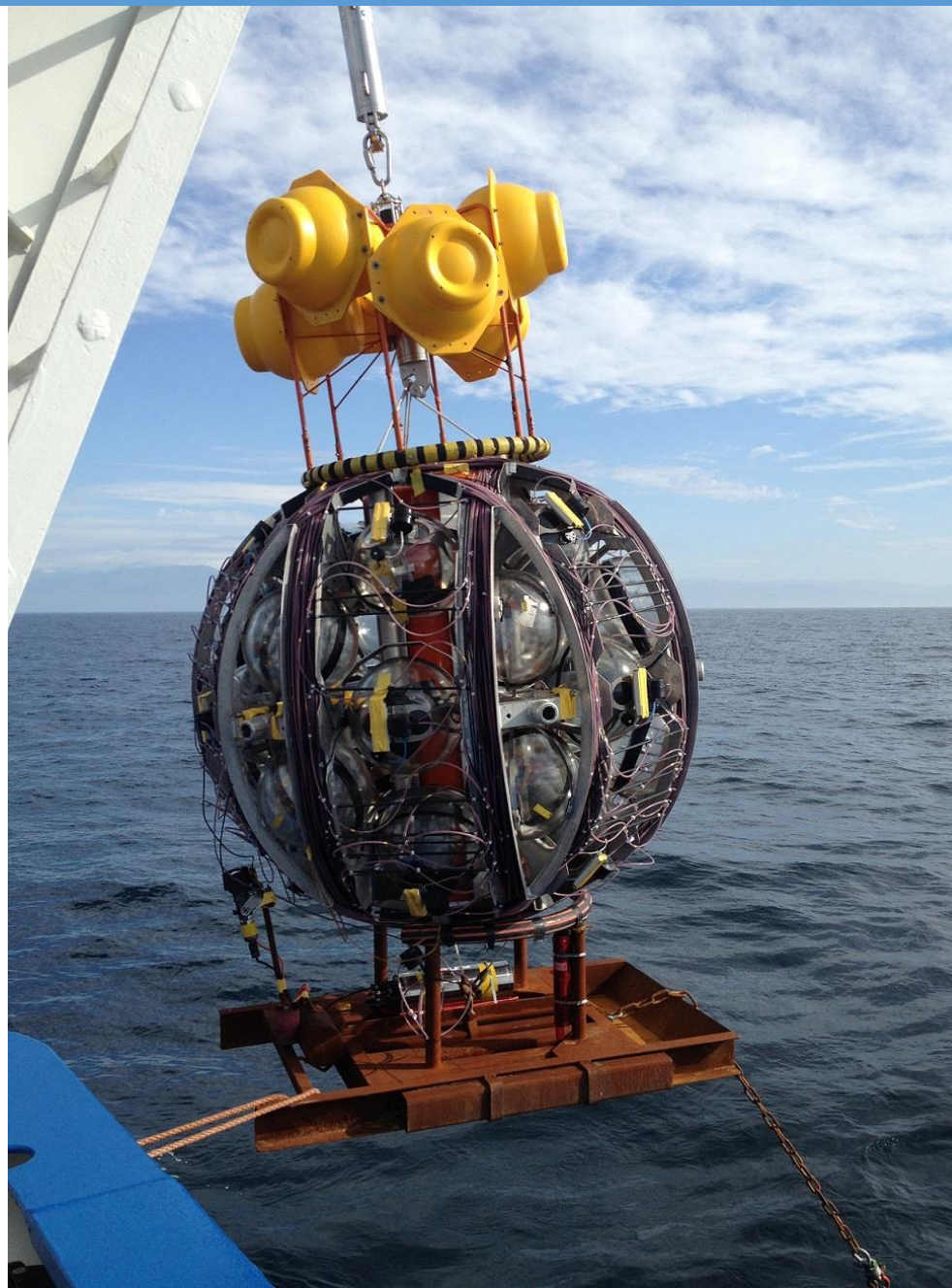
Detection Unit (**DU**):  
vertical **string** with 18 DOMs

Eur. Phys. J. C 76 (2016) 76:54

Naming:

ORCA6 ↔ ORCA with 6 strings  
ARCA2 ↔ ARCA with 2 strings  
etc.

2020 JINST 15 P11027



© Marijn van der Meer/Quest



Detection Unit (**DU**):  
vertical **string** with 18 DOMs

Eur. Phys. J. C 76 (2016) 76:54

Naming:

**ORCA6** ↔ **ORCA** with 6 strings  
**ARCA2** ↔ **ARCA** with 2 strings  
etc.

2020 JINST 15 P11027



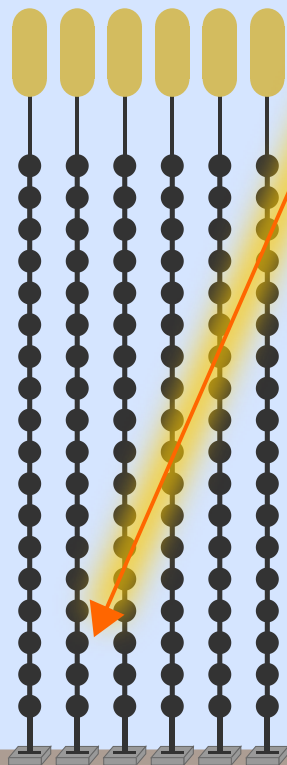


Examples of basic event topologies:

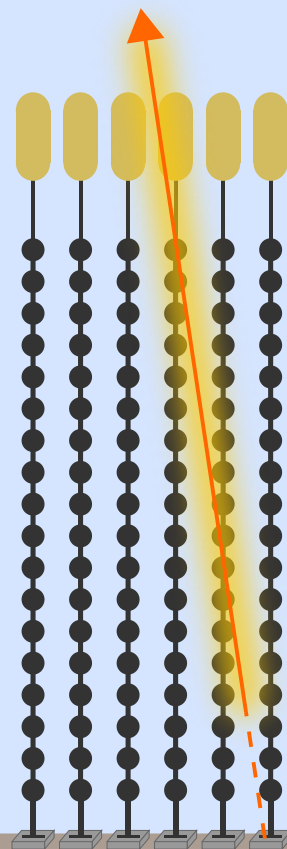
Classes based on combinations of:

- ❖ Direction
- ❖ Shape

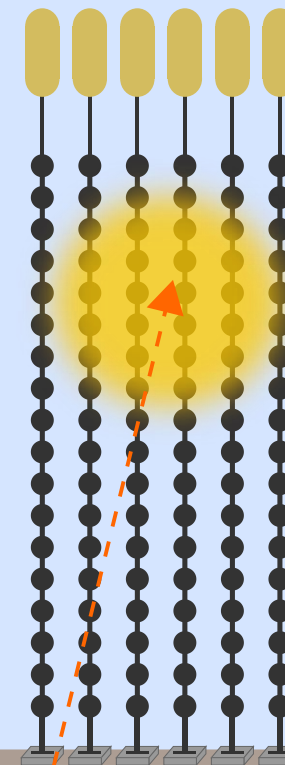
down-going track  
(typically atm.  $\mu$ )



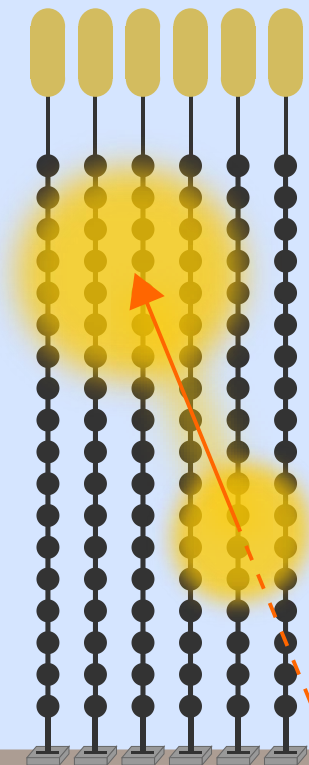
up-going track  
(typically atm.  $\nu_\mu$ )



single cascade  
(typically atm.  $\nu_e/\nu_\tau$ )

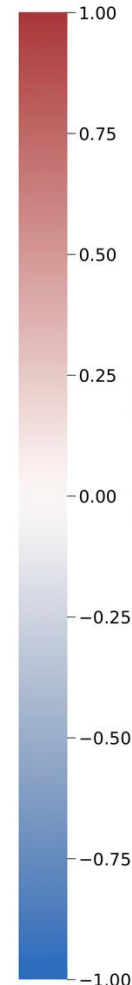


double cascade  
(typically atm.  $\nu_\tau$ )



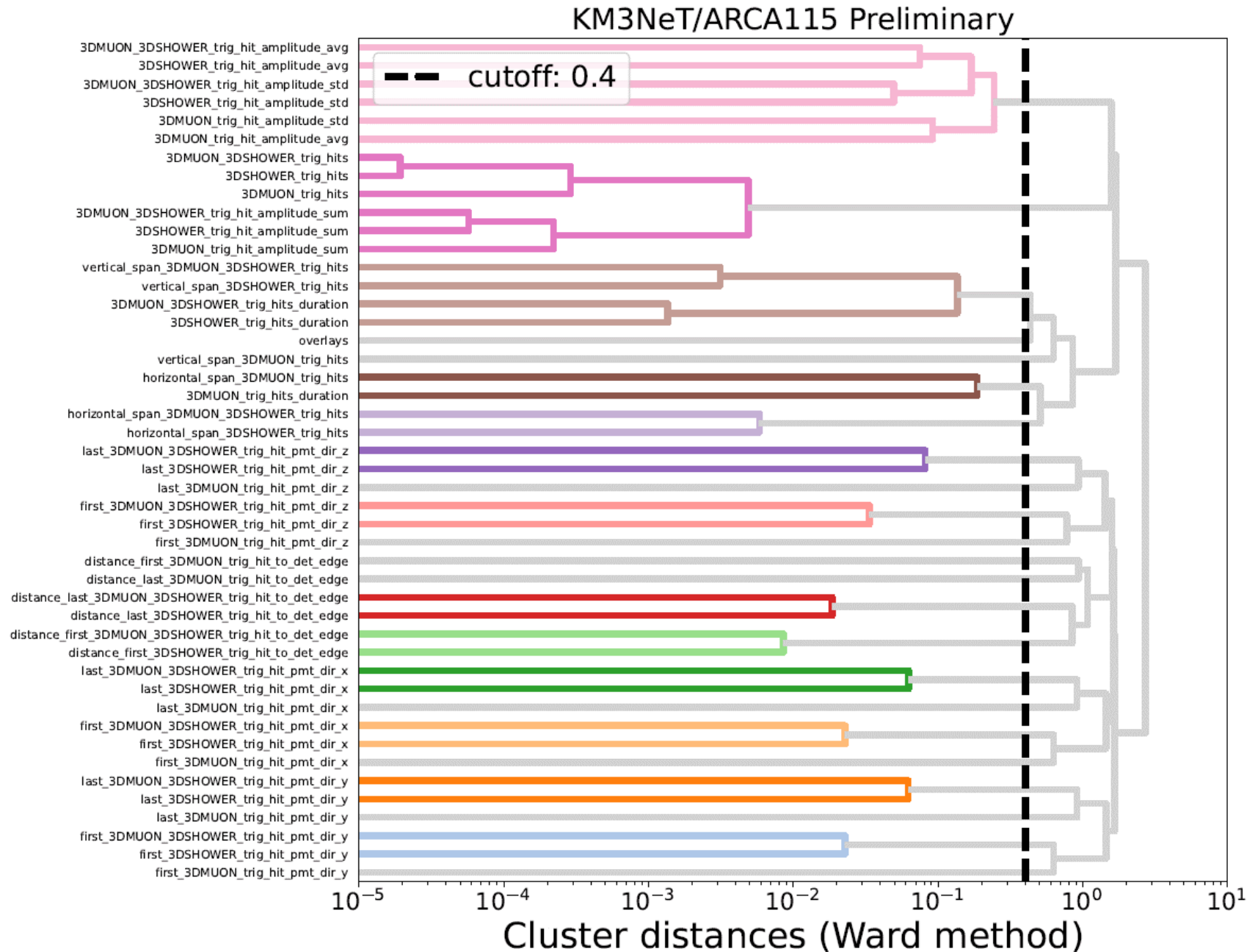
seabed

-0.0	-0.1	-0.0	0.0	-0.1	0.4	0.0	0.1	-0.0	-0.0	-0.1	-0.0	0.0	-0.1	0.5	-0.1	0.0	0.0	-0.0	-0.1	-0.0	0.0	-0.1	0.4	1.0	1.0
0.0	0.0	-0.0	0.0	0.0	-0.1	0.3	0.0	0.1	0.0	0.0	-0.1	-0.0	0.0	0.3	-0.1	-0.1	-0.0	0.0	-0.0	0.0	0.0	-0.1	0.3	0.3	0.0



In total: 46 features (+4 targets)

Example for ARCA115  
(the same was done for ARCA6,  
ORCA115 and ORCA6)



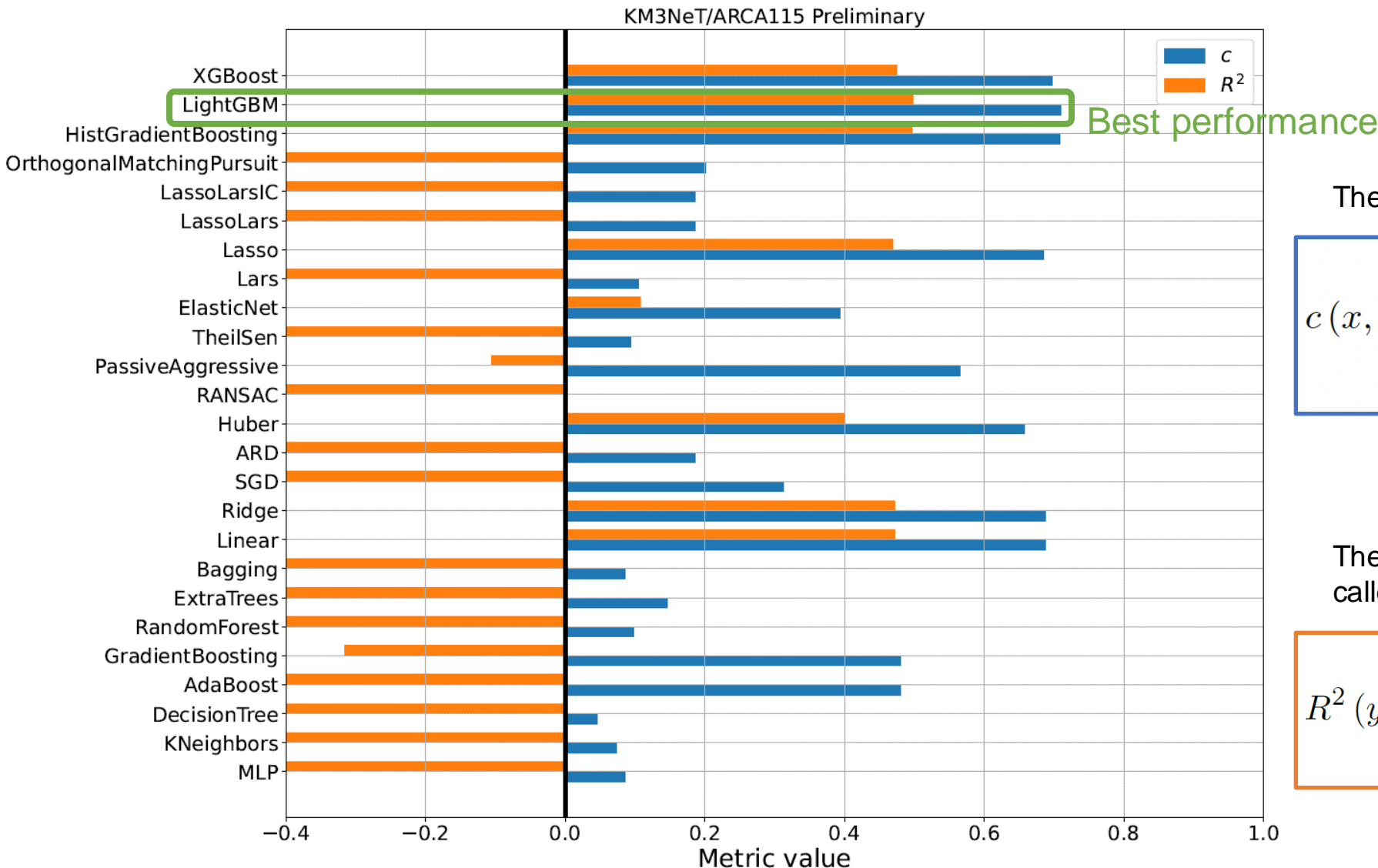
Cluster distance cutoff is arbitrary

Clusters are marked by different colors

Example for ARCA115  
(the same was done for ARCA6,  
ORCA115 and ORCA6)



Performance comparison on a fraction (50k events) of the training dataset:



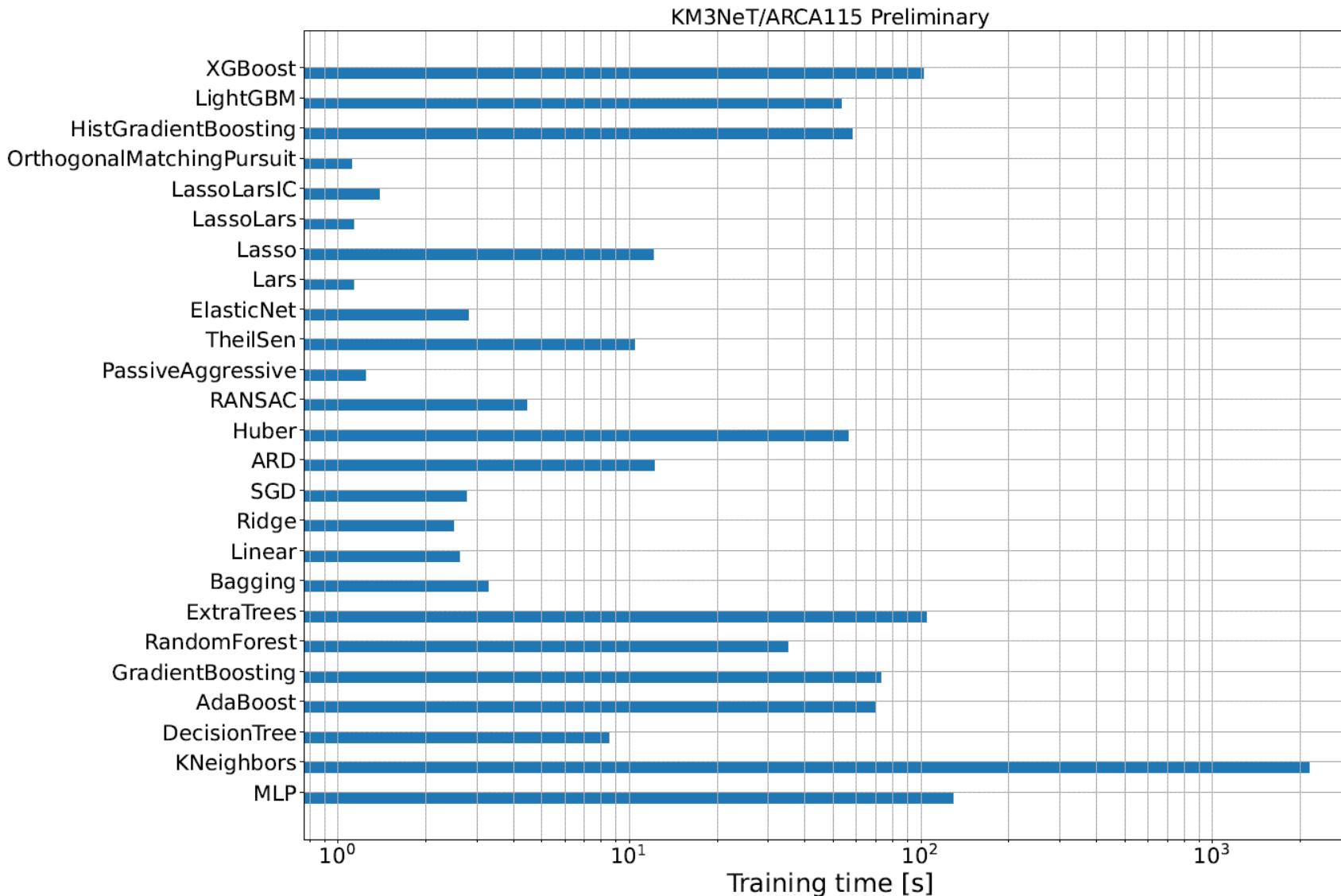
The (weighted) Pearson correlation coefficient:

$$c(x, y) = \frac{\sum_i w_i (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum_i w_i (x_i - \bar{x})^2 \sum_i w_i (y_i - \bar{y})^2}}$$

The (weighted) R2-score,  
called the coefficient of determination:

$$R^2(y_{\text{true}}, y_{\text{pred}}) = 1 - \frac{\sum_i w_i (y_{\text{true}} - y_{\text{pred}})^2}{\sum_i w_i (y_{\text{true}} - \bar{y})^2}$$

Speed comparison on a fraction (50k events) of the training dataset:

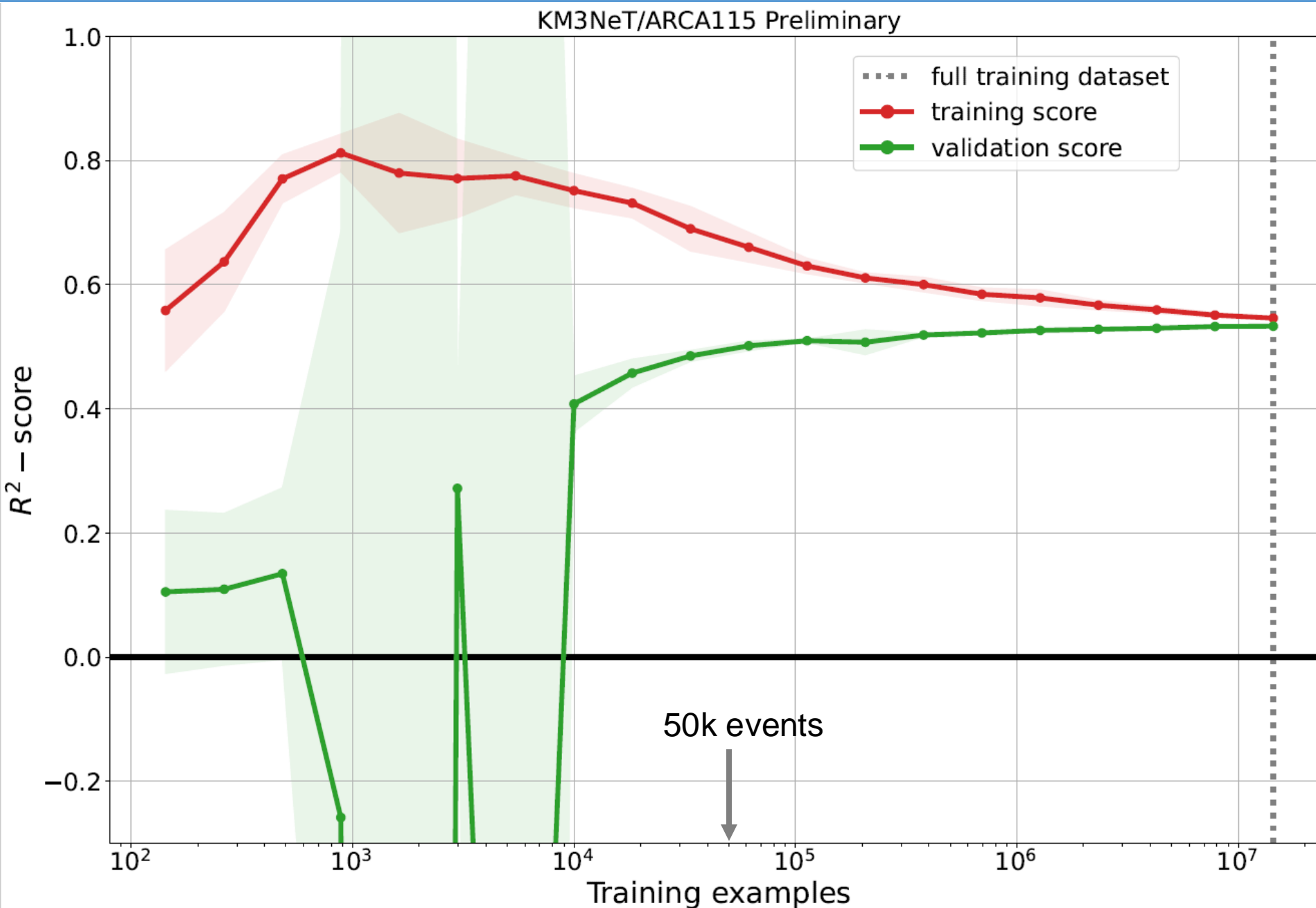


LightGBM:

- ❖ not the fastest, but still very decent
- ❖ + it turned out to scale up very well (entire dataset is orders of magnitude larger)

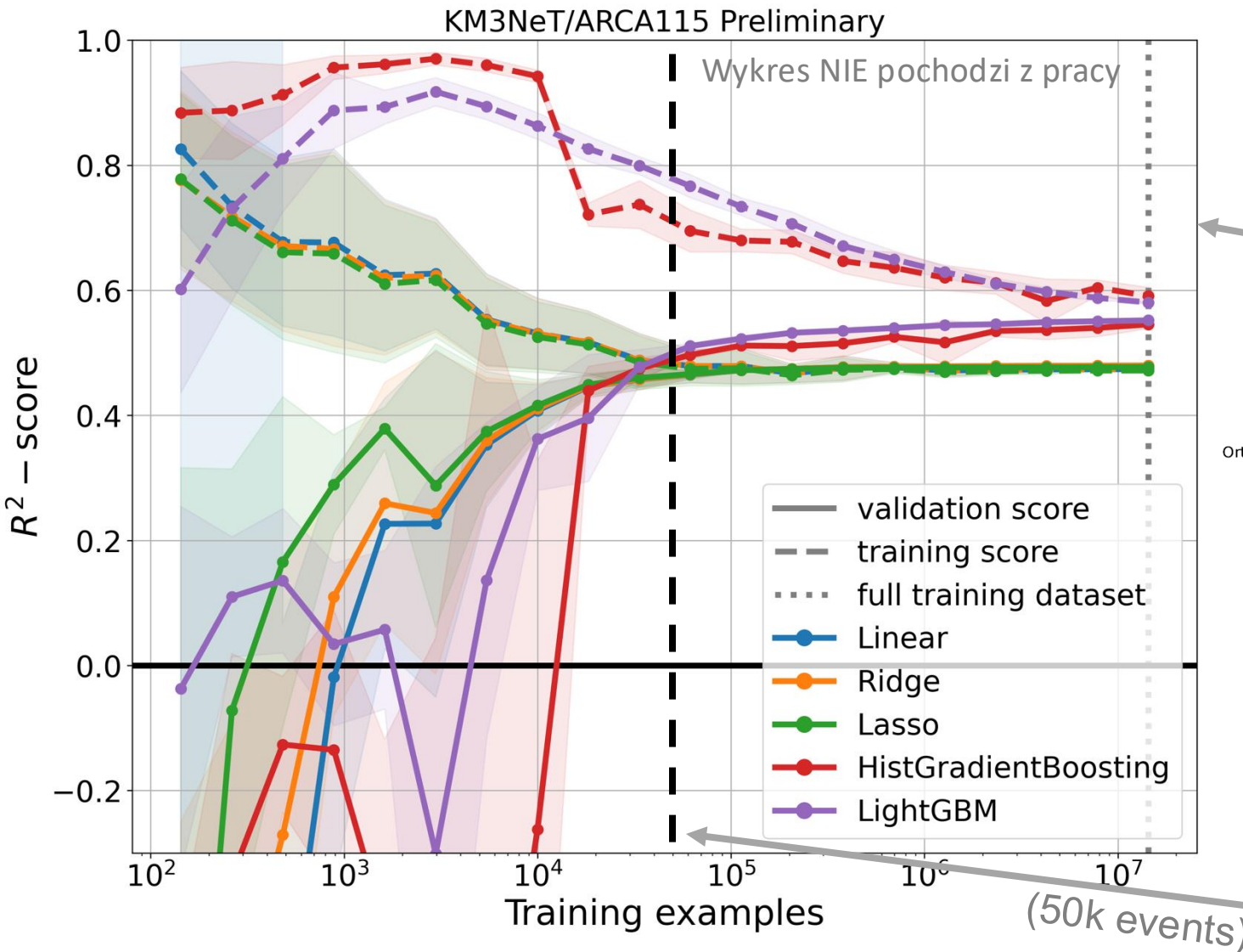
These times were obtained running with 20 CPU cores in parallel



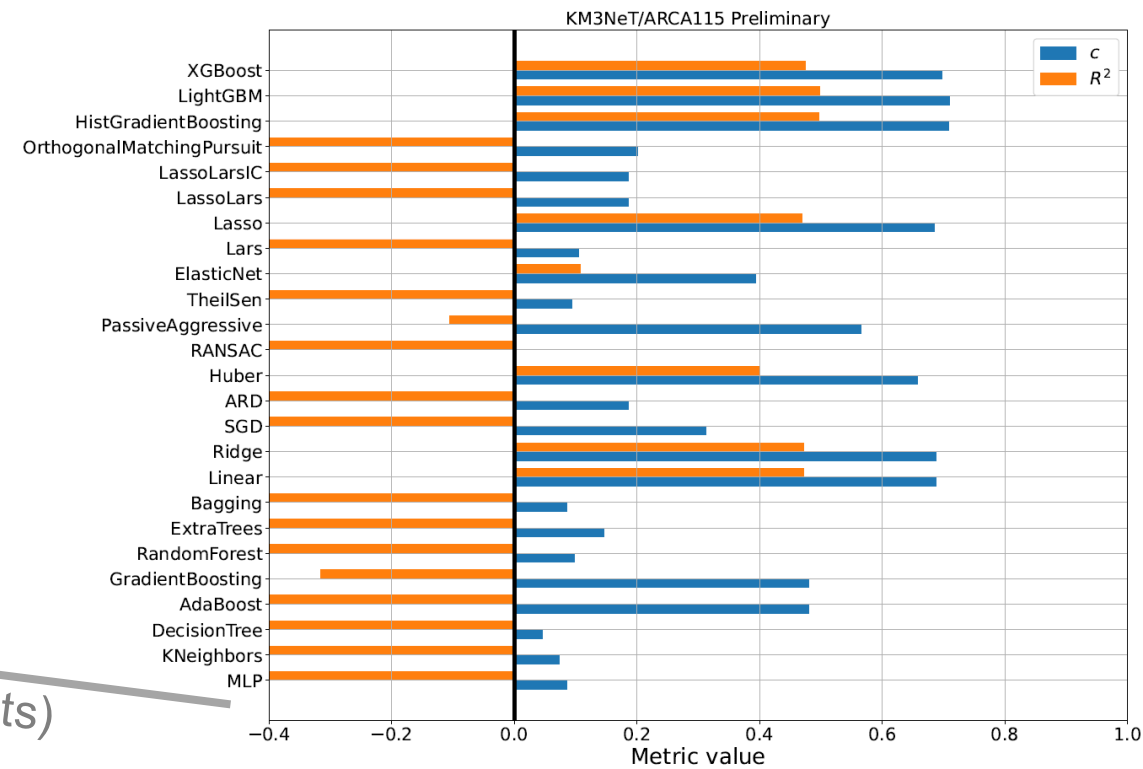


Here we see why 50k events were fine for testing (but e.g. 5k would not be)

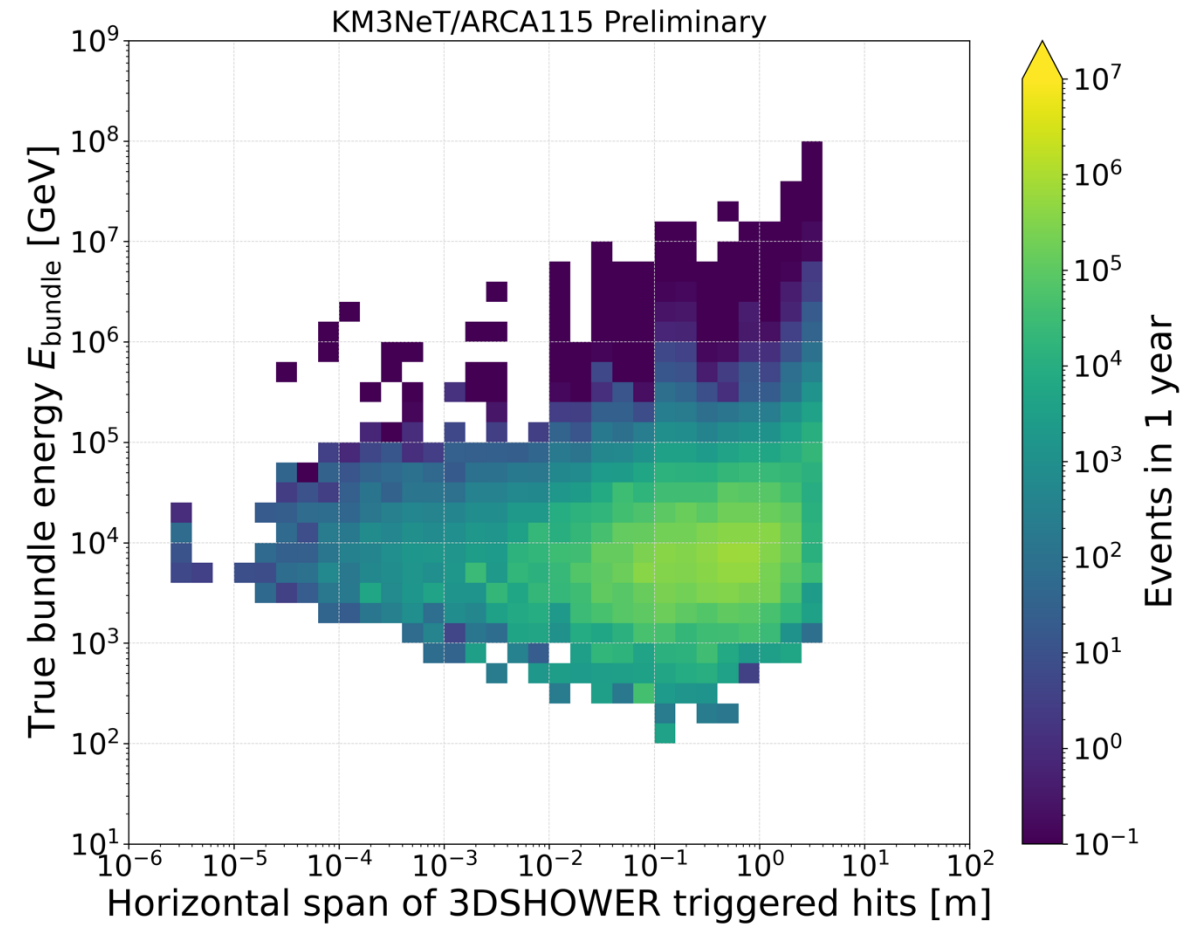
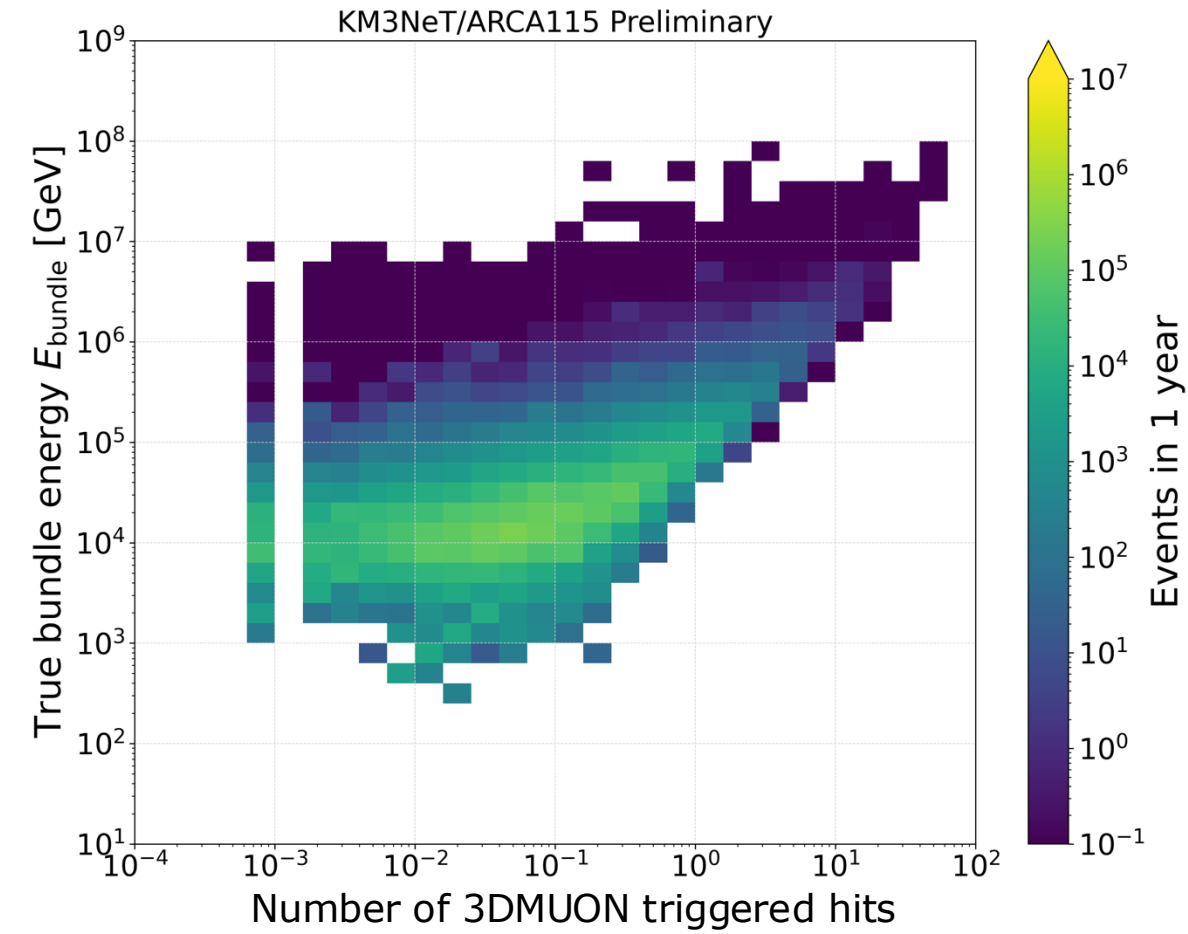
Linear does almost as good as LightGBM:

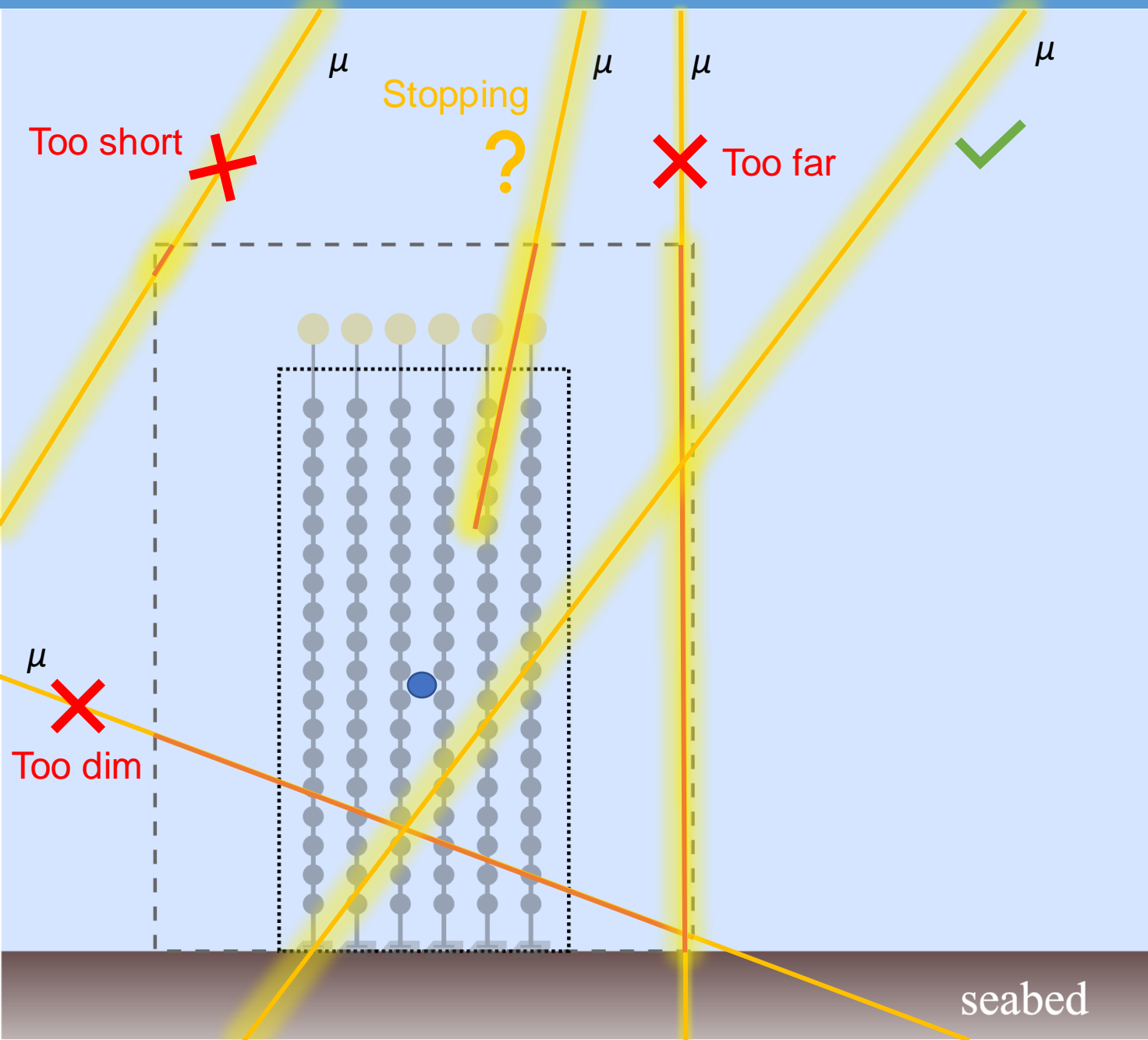


same hyperparameters



- ❖ Performance of Linear could not be further improved:
  - Flat learning curve (NOT for LightGBM!)
  - No hyperparameters to tune
- ❖ Reconstructed observables are non-linear functions of features:  
(so Linear has no chance to fully describe them)





We want to exclude muons, which:

- ❖ Are too far from the detector
- ❖ Have too short pathlength inside the volume of interest
- ❖ Emit too faint light (have too low Energy)
- ❖ Basically are not visible or would be poorly reconstructed

How?

- ❖ Check the JMuon\* likelihood  $\mathcal{L}$  for single muon events against:
  - distance of muon from the DET center (●) for vertical muons → pick an optimal volume by shrinking the can by  $x$  as:
 
$$r_{\text{can}} - x, h_{\text{can}} - x$$
  - muon pathlength  $L$  but for shrunked can
  - muon energy →  $E$  cut

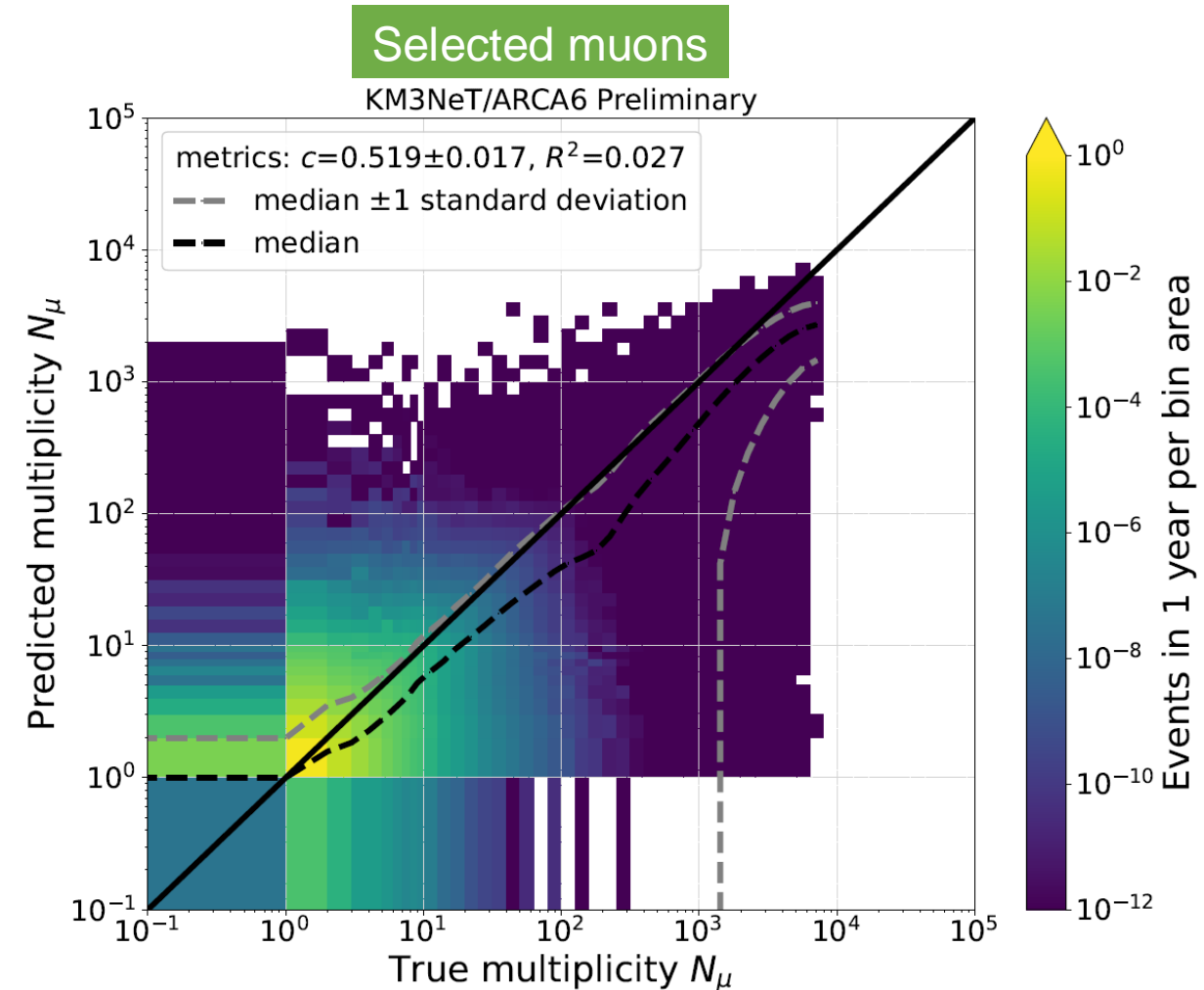
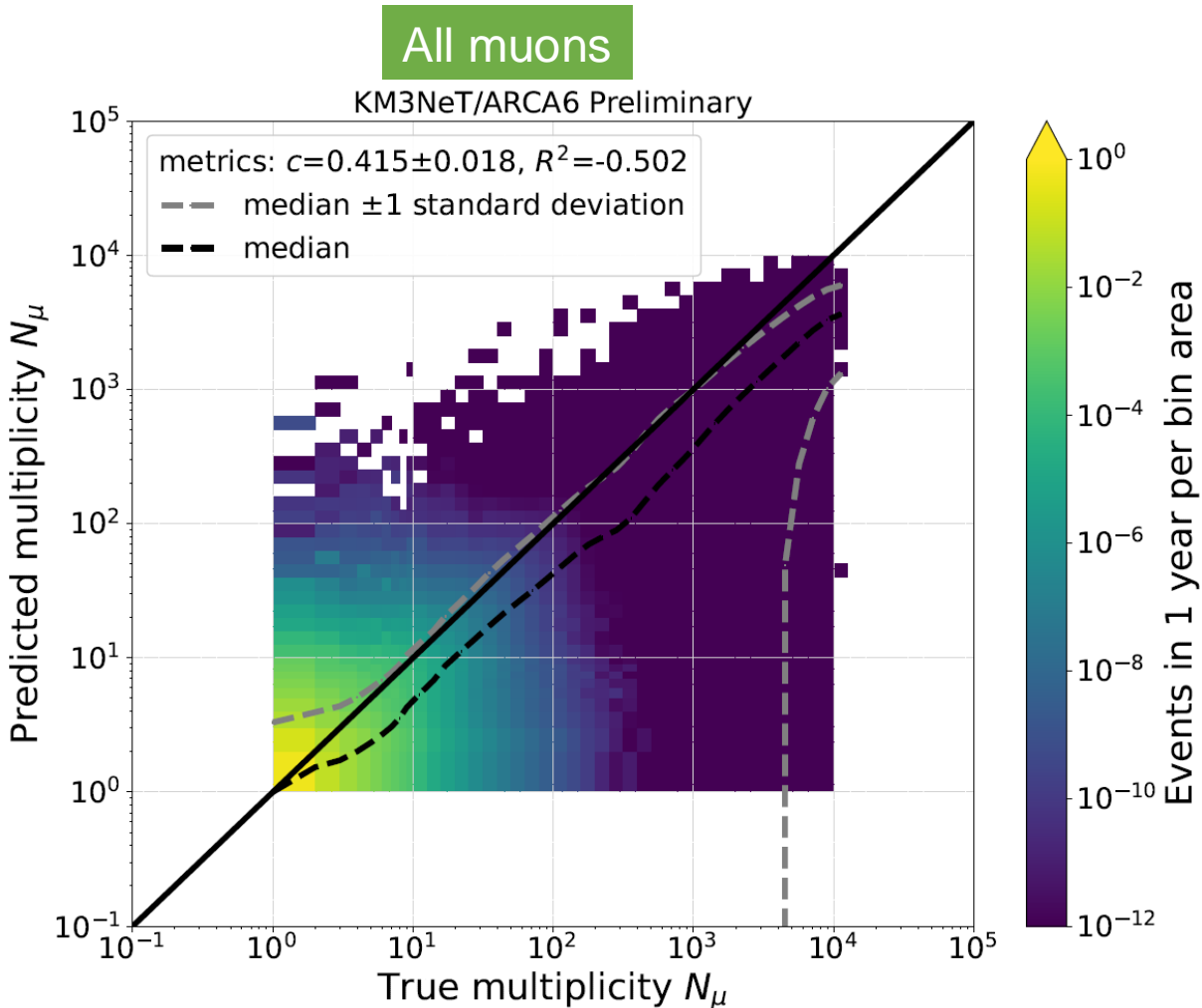
Summary of the selection:

Detector	Minimal $E_\mu$ [GeV]	$d_{\max}$ [m]	minimal $L_\mu$ [m]
ARCA115	120	-	-
ARCA6	120	269.4	240
ORCA115	1	-	-
ORCA6	1	-	-

This selection is used for further multiplicity results



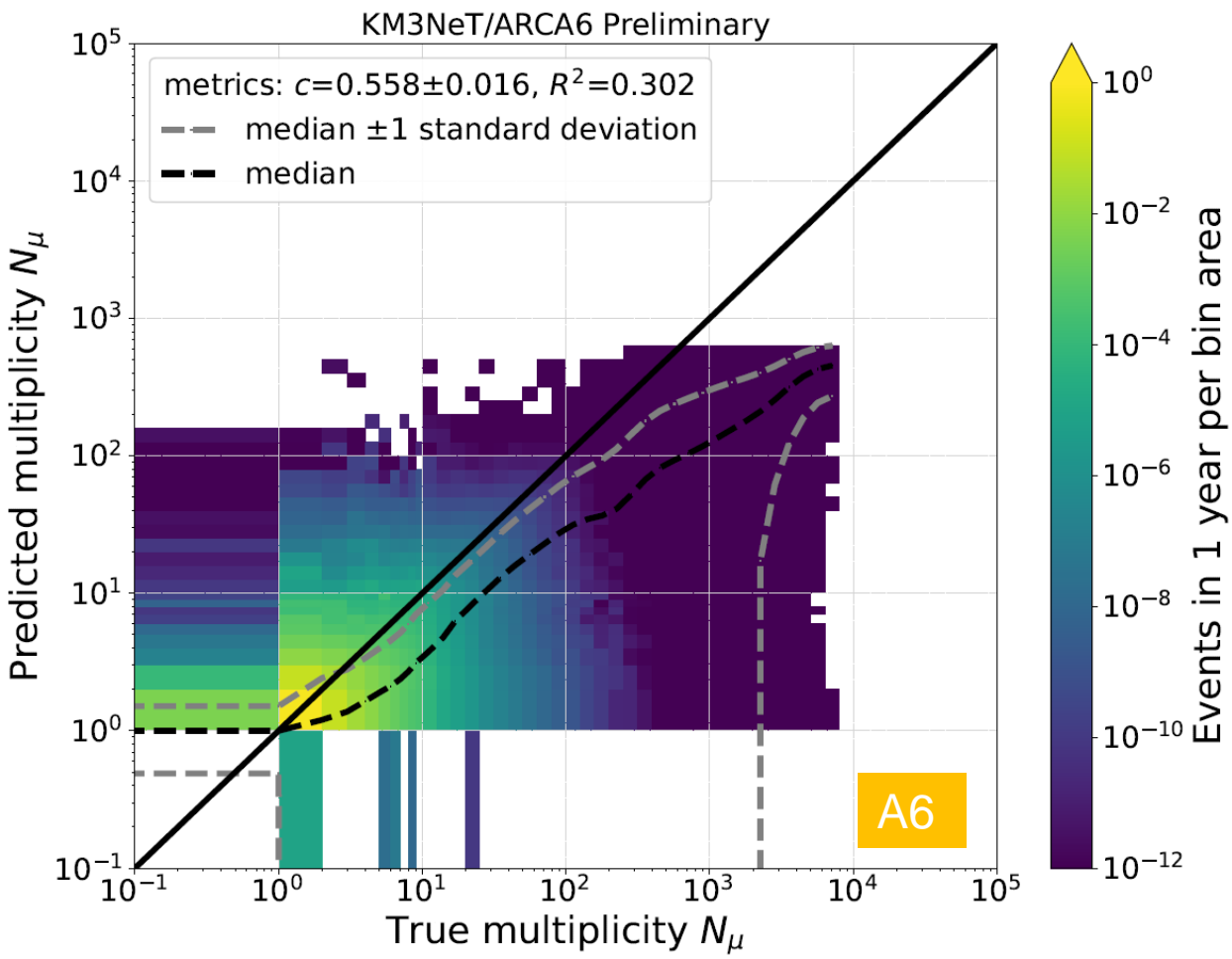
Example of ARCA6, for which the effect is the most pronounced



Analogical results obtained for ARCA115, ORCA115 and ORCA6

## Example of the results for ARCA6:

2D: pred vs true



1D histograms

